

ISPR 2017 TU WIEN, Sept 2017



Department of Mechanical Engineering

## Structural Integrity of Complex Components by Means of the Strain Energy Density Approach

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Chair of Mechanics and Materials

Professor of Fatigue Design

Norwegian University of Science and Technology



# INTERNATIONAL SYMPOSIUM FOR PRODUCTION RESEARCH 2017

## “Transition to Industry 4.0”

13-15 September 2017, Vienna



TECHNISCHE  
UNIVERSITÄT  
WIEN

### ISPR 2017

13-15 September 2017, Vienna



Üretim Araştırmaları  
Derneği

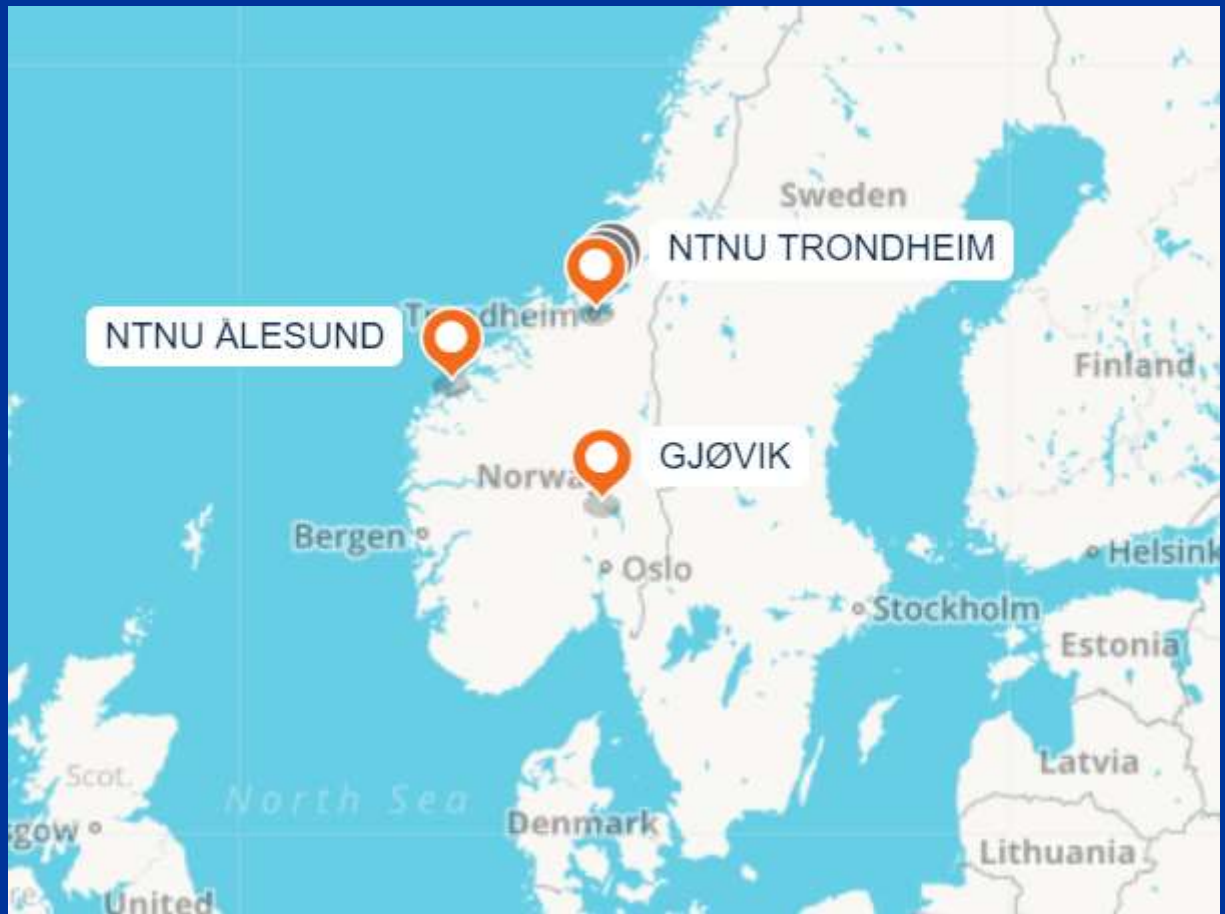
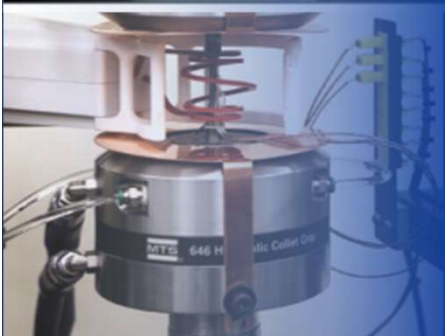
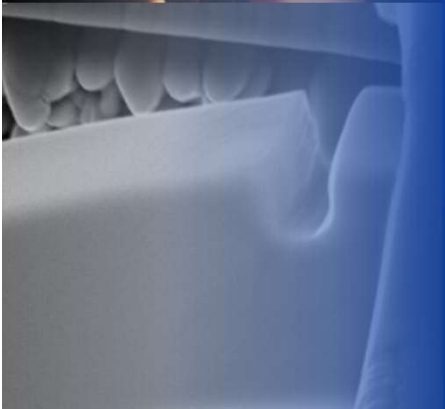


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# Outline of Presentation

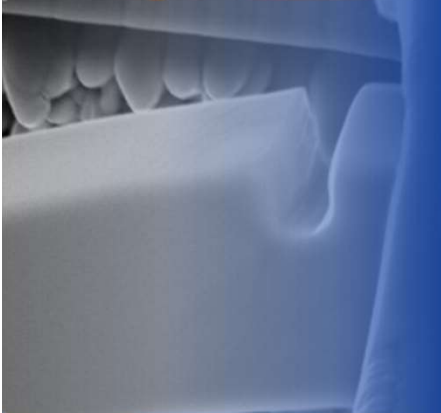
- Introduction
- Objectives
- Theoretical Background
- Testing
- SED applied for fatigue assessment
- Ongoing projects







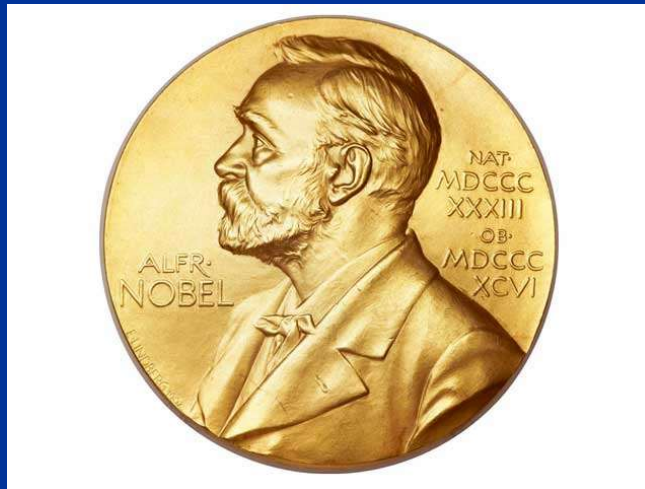
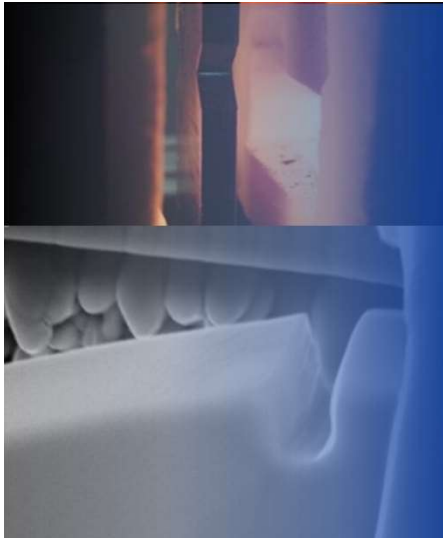
**30000 students**  
**40 faculties**  
**Nobel prize award 2014**



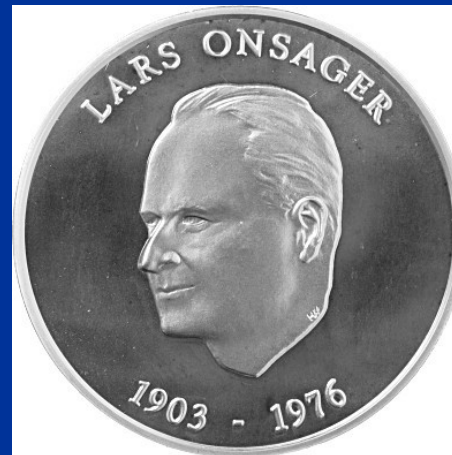


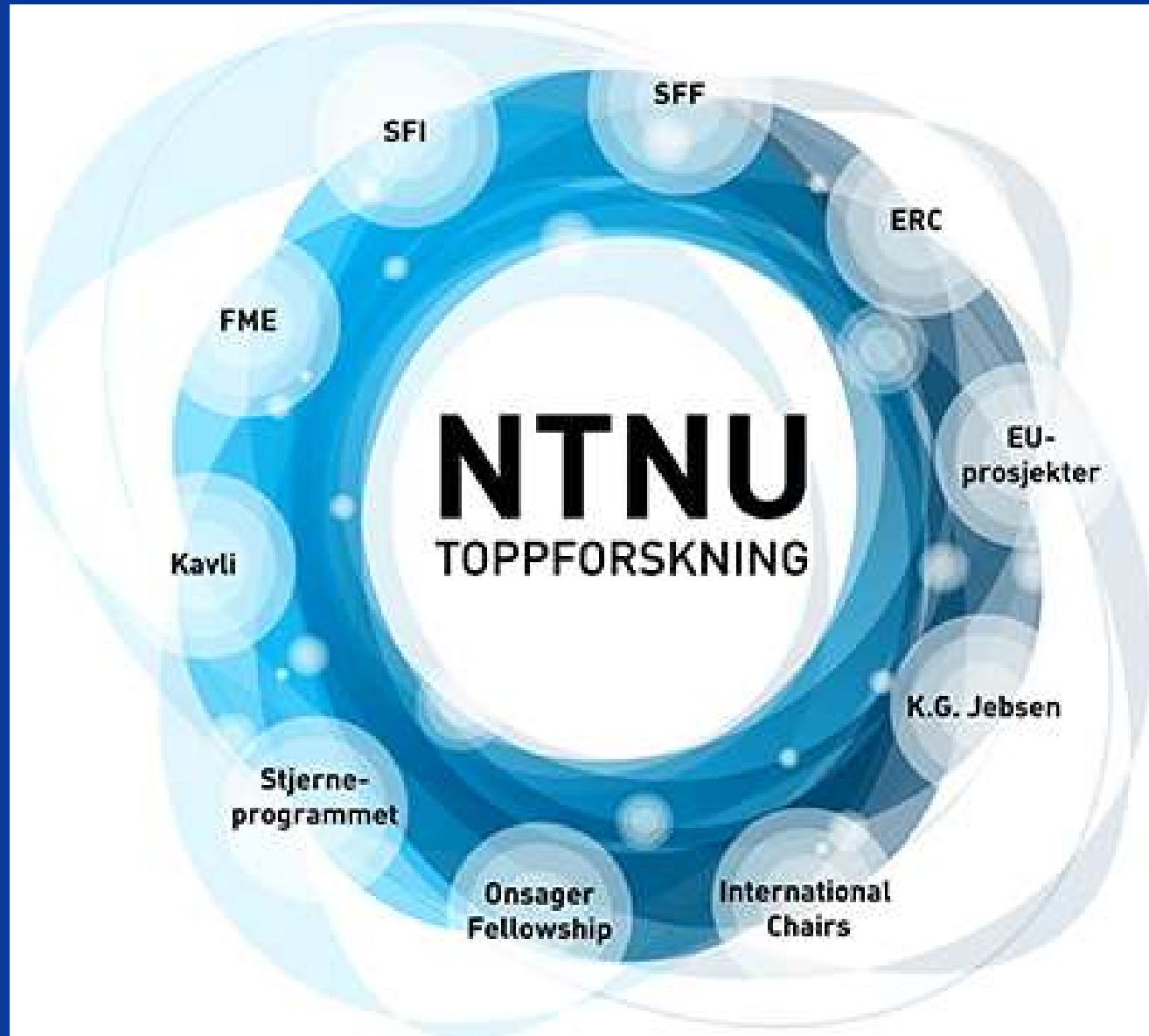
**30000 students**  
**40 faculties**  
**Nobel prize award 2014**





- 1968 Lars Onsager, Chemistry 🏆 (graduate engineer from Norwegian Institute of Technology, NTH, in 1925)
- 1973 Ivar Giaever, Physics 🏆 (graduate engineer from Norwegian Institute of Technology, NTH, in 1952)
- 2014 Edvard Moser, Medicine or Physiology 🏆 (professor of neuroscience, NTNU)
- 2014 May-Britt Moser, Medicine or Physiology 🏆 (professor of neuroscience, NTNU)
- 2014 John O'Keefe, Medicine or Physiology 🏆 <sup>[31]</sup> (visiting researcher, NTNU 2015– )









Stephen Hawking



Buzz Aldrin



May-Britt Moser



Emmanuelle Charpentier



Claude Nicollier  
Astronaut



Katharine Hayhoe  
Atmospheric scientist



Sara Seager  
Planetary scientist



Oliver Stone  
Director and writer





# Structural Mechanics and

# Materials Research Group



Department of Mechanical Engineering

## Staff in my group:

3 Academics

2 Research Fellows

~ 10 PhD students

Supported by workshop and admin staff

## Research Directions:

Fatigue of metallic and non metallic materials

Solid and Fracture Mechanics

Structural Integrity of welding under fatigue loadings

Material Science

Full scale testing

Structural Health Monitoring



# Structural Mechanics and Materials Research Group

## Facilities:

Welding facilities

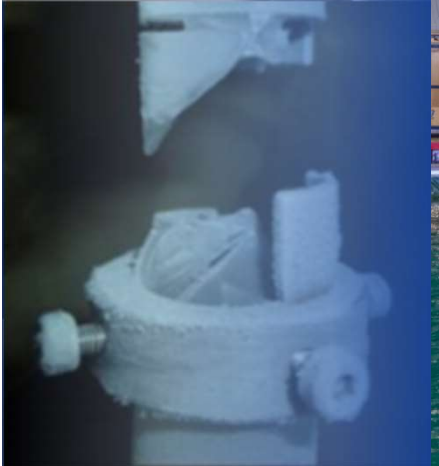
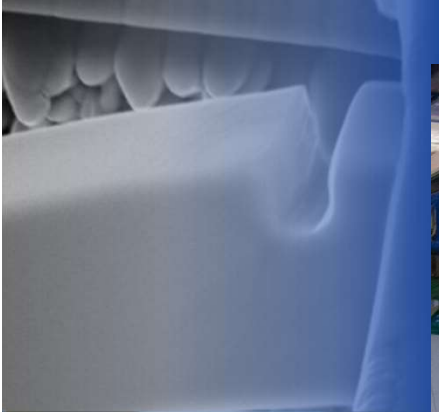
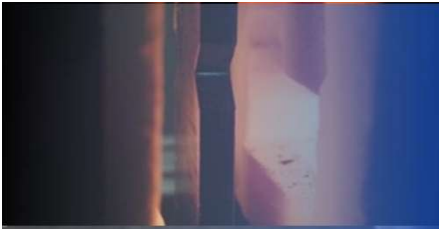
Mechanical testing capabilities (more than 80 MEuro)

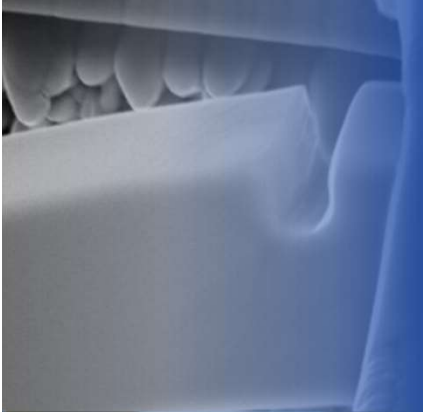
NanoLab

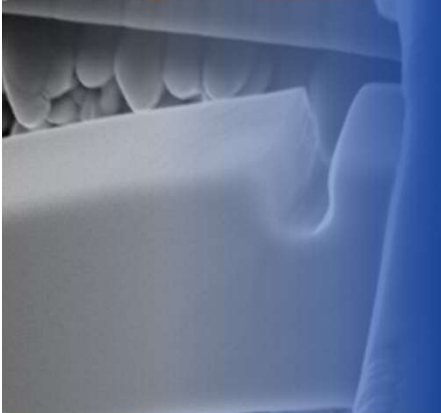
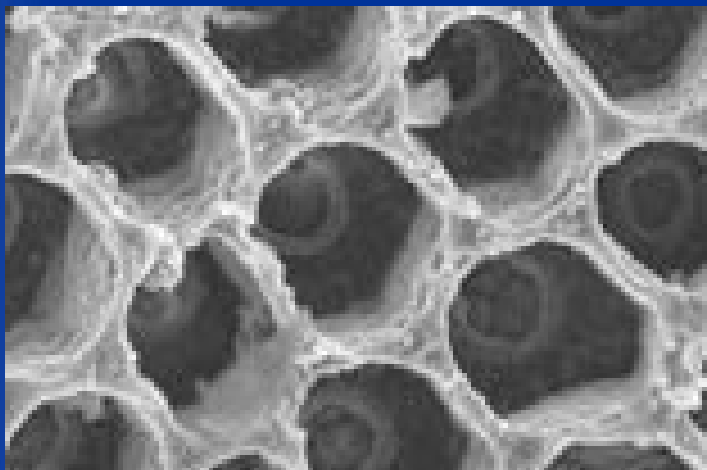
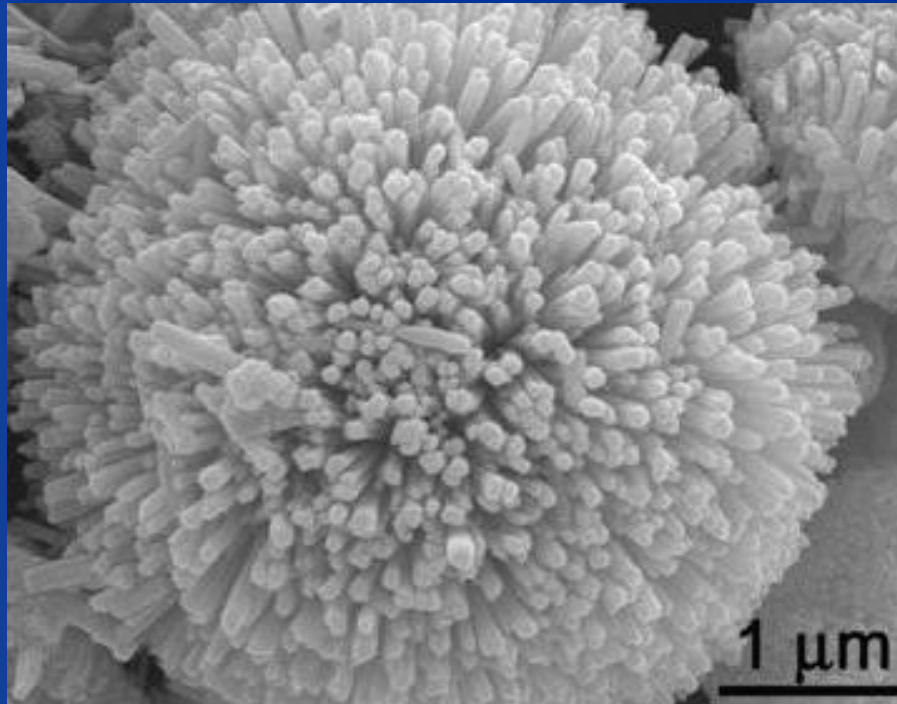
Lazzarin fatigue Lab (15 MEuro)

## Collaboration:

Collaborative work with Norwegian, Australian, European, Canadian and South Korean Universities and Research Centres



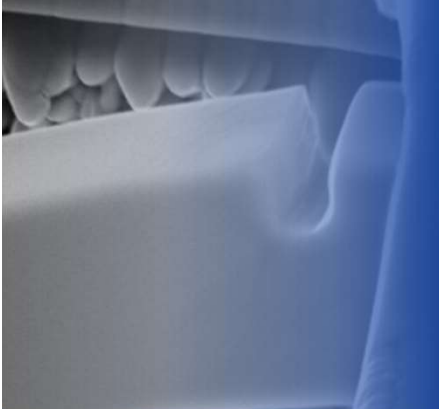





# OBJECTIVES



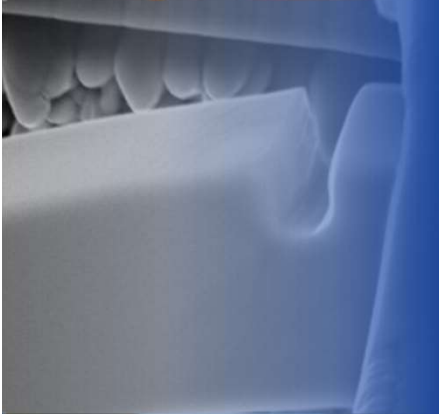
The present work investigates the multiaxial fatigue strength of sharp V-notched components made of titanium grade 5 alloy (Ti-6Al-4V).



Axi-symmetric notched specimens have been tested under combined tension and torsion fatigue loadings, both proportional and non-proportional, taking into account different nominal load ratios ( $R = -1$  and  $R=0$ ) and biaxiality ratios ( $\lambda=\tau/\sigma=2$  and  $0.6$ ). All tested samples have a notch root radius about equal to  $0.1$  mm, a notch depth of  $6$  mm and an opening angle of  $90$  degrees.



Altogether, more than  $250$  fatigue results ( $19$  S-N curves) are examined, first on the basis of nominal stress amplitudes referred to the net area and secondly by means of the strain energy density averaged (Lazzarin and Zambardi, 2001) over a control volume embracing the V-notch tip.





# Strain Energy Density

- Beltrami E (1885)** Sulle condizioni di resistenza dei corpi elastici, Rend. R. Ist. Lombardo di Scienze, Lettere e Arti, 18, 704 (in Italian)
- Gillemot L (1965)** Brittle fracture of welded materials. Commonwealth Welding Conference C.7.353-358.
- Gillemot L (1976)** Criterion of crack initiation and spreading, Engng Fract Mech 8 239-253.
- Gillemot L, Czoboly E and Havas I (1985)** Fracture mechanics applications of absorbed specific fracture energy: Notch and unnotched specimens Theor Appl Fract Mech 4 39-45
- Sih GC (1974)** Strain-energy-density factor applied to mixed mode crack problems. Int J Fract 10 305-321.
- Sih GC (1991)** Mechanics of Fracture Initiation and Propagation: Surface and volume energy density applied as failure criterion, Kluwer Academic Publisher, Dordrecht
- Sih GC, Tang XS (2005)** Scaling of volume energy density function reflecting damage by singularities at macro-, meso- and microscopic level. Theor Appl Fract Mech 43 211-231.
- Sih GC (2007)** Multiscaling in molecular and continuum mechanics: interaction of time and size from macro to nano. Dordrecht: Springer.
- Sih G.C. (2011)** Pseudo global energy released locally by crack extension involving multiscale reliability Theoretical and Applied Fracture Mechanics 55 (2011) 52-59
- Ellyin F., Kujawski D (1989)** Generalization of notch analysis and its extension to cyclic loading, Engineering Fracture Mechanics 32 819-826
- Ellyin F (1997)** Fatigue Damage, Crack Growth and Life Prediction, Chapman & Hall, London
- Glinka G (1985)** Energy density approach to calculation of inelastic strain-stress near notches and cracks Engng Fract Mech 22 485-508.
- Gdoutos EE (1990)** Fracture Mechanics Criteria and Applications, Dordrecht: Kluwer Academic Publishers; 1990.
- Park J, Nelson D (2000)** Evaluation of an energy-based approach and a critical plane approach for predicting constant amplitude multiaxial fatigue life. Int J Fatigue 22 23-39.

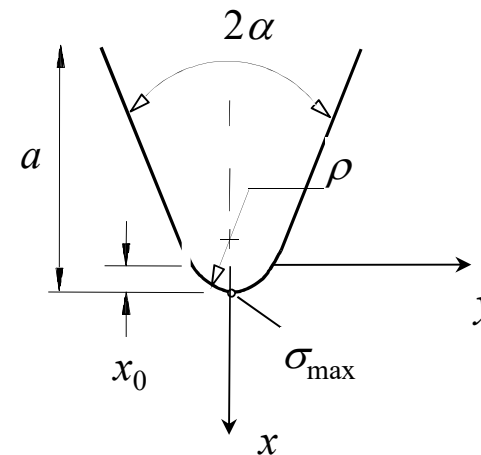
# VARIATION OF THE STRAIN ENERGY DENSITY AT THE NOTCH TIP FOR BLUNT NOTCHES

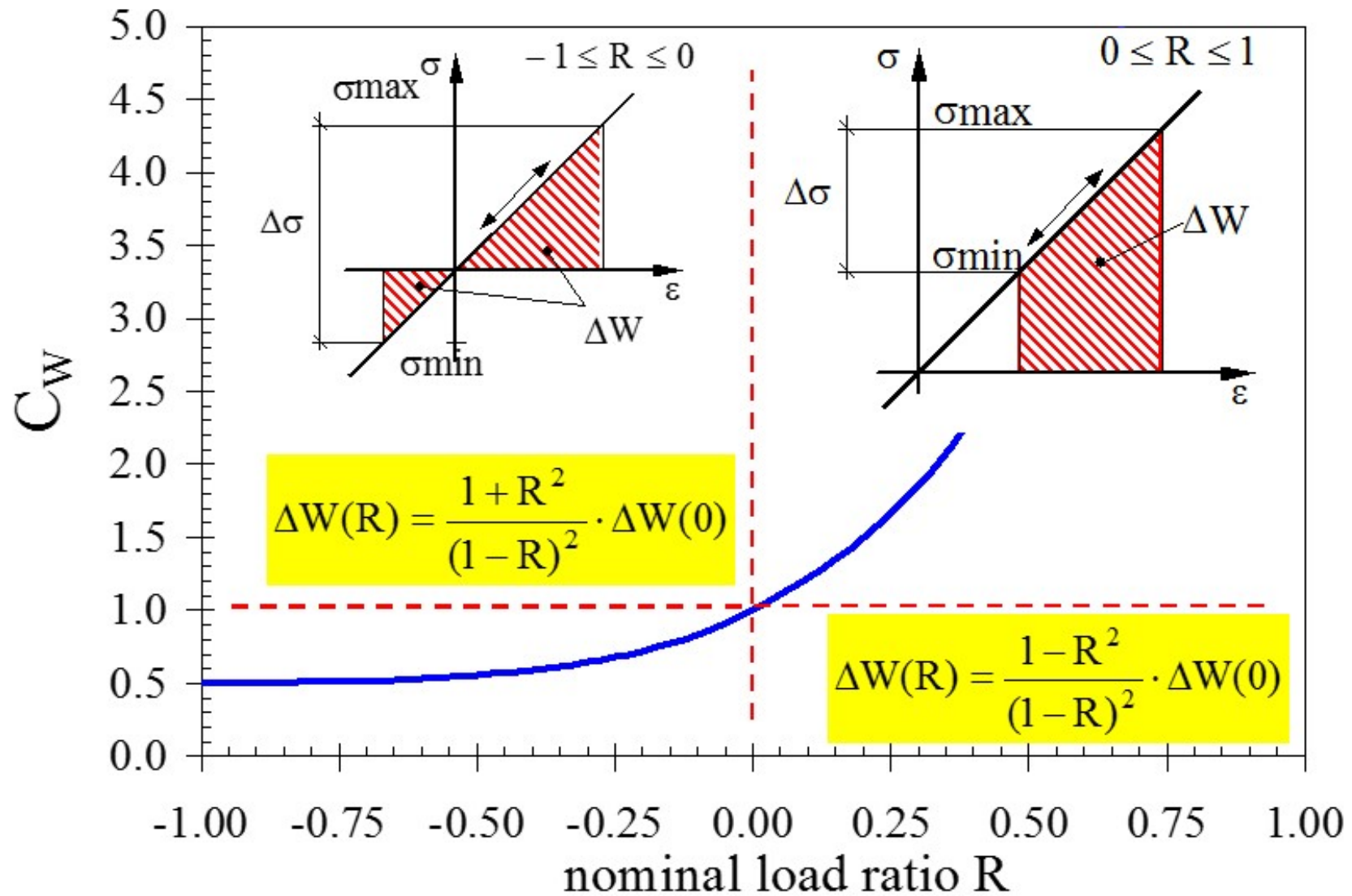
$$W^{(e)} = \frac{1}{2E} \left[ \sigma_{rr}^2 + \sigma_{\theta\theta}^2 + \sigma_{zz}^2 - 2\nu(\sigma_{rr}\sigma_{\theta\theta} + \sigma_{rr}\sigma_{zz} + \sigma_{\theta\theta}\sigma_{zz}) + 2(1+\nu)(\sigma_{r\theta}^2 + \sigma_{rz}^2 + \sigma_{\theta z}^2) \right]$$

$$\Delta W_t = c_w \cdot \frac{1}{2 \cdot E} \cdot \left( \Delta \sigma_{p,el}^2 + 2 \cdot (1 + \nu) \cdot \Delta \tau_{p,el}^2 \right)$$

$$\Delta W_t = c_w \cdot \frac{1}{2 \cdot E} \cdot \left( k_{t \text{ net, ax}}^2 \cdot \Delta \sigma_{\text{net}}^2 + 2 \cdot (1 + \nu) \cdot k_{t \text{ net, tors}}^2 \cdot \Delta \tau_{\text{net}}^2 \right)$$

$$c_w(R) = \begin{cases} \frac{1+R^2}{(1-R)^2} & \text{if } -1 \leq R < 0 \\ 1 & \text{if } R = 0 \\ \frac{1-R^2}{(1+R)^2} & \text{if } 0 < R \leq 1 \end{cases}$$



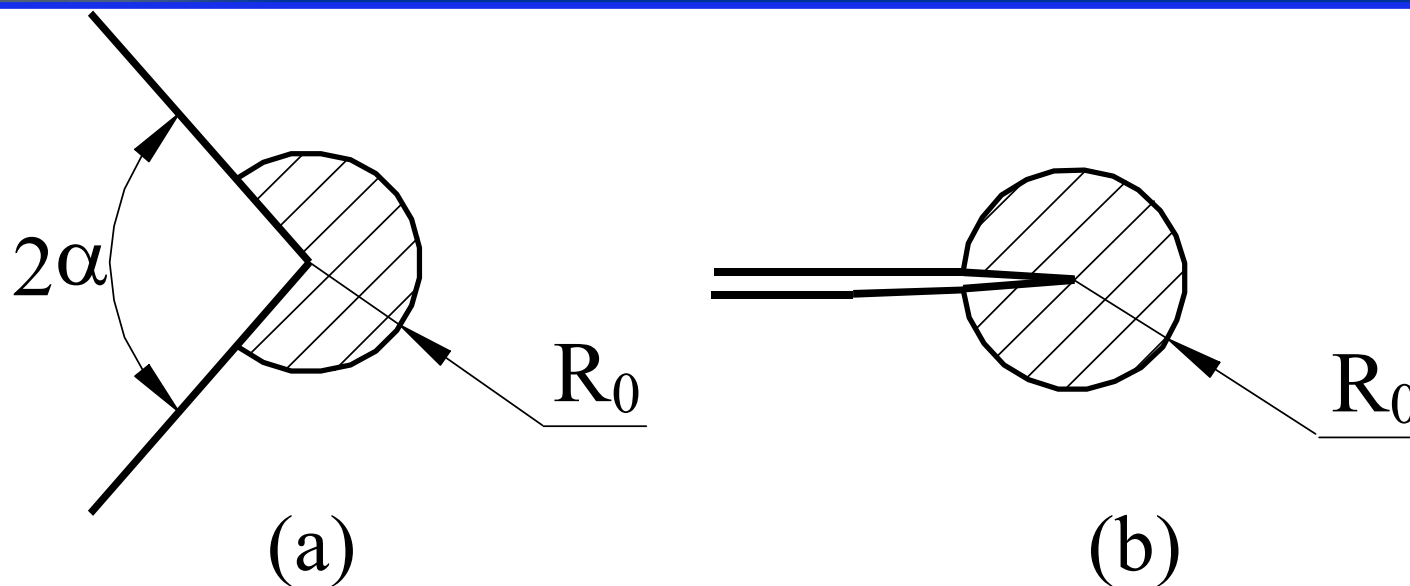


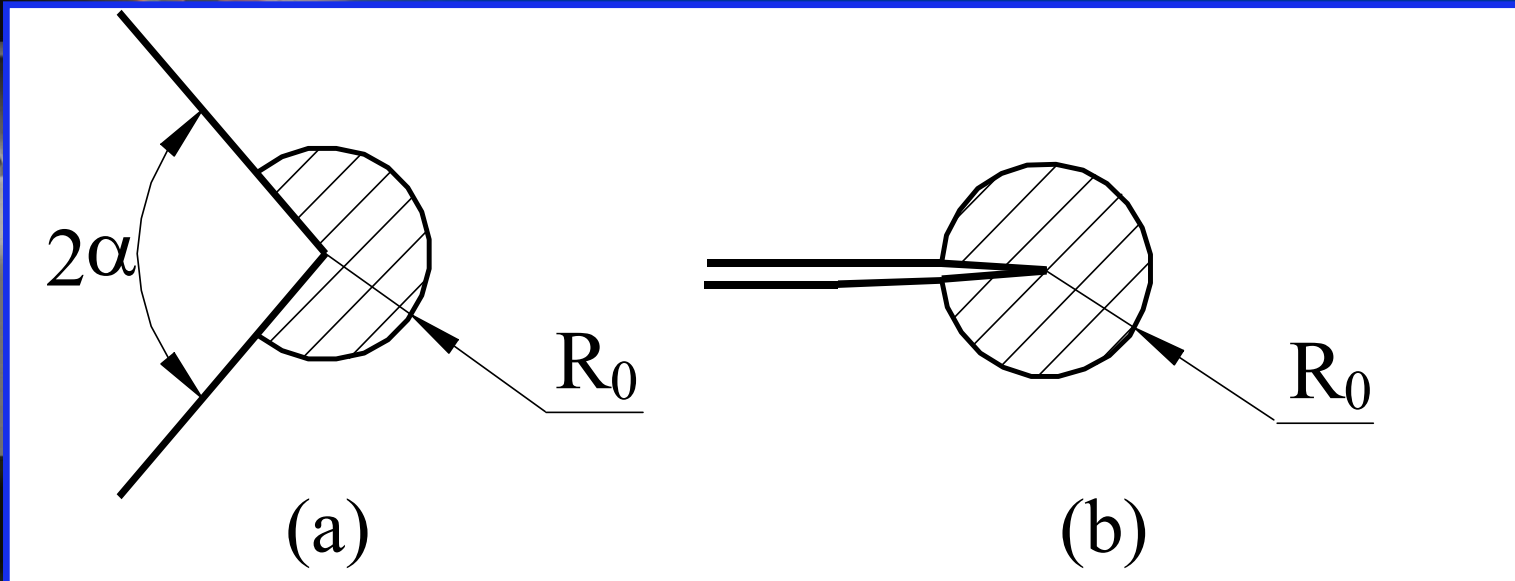
## Analytical background

$$W(r, \theta) = W_1(r, \theta) + W_2(r, \theta) + W_{12}(r, \theta)$$

$$W_1(r, \theta) = \frac{1}{2E} r^{2(\lambda_1-1)} \cdot (K_1^N)^2 \left[ \tilde{\sigma}_{\theta\theta}^{(1)2} + \tilde{\sigma}_{rr}^{(1)2} + \tilde{\sigma}_{zz}^{(1)2} - 2\nu(\tilde{\sigma}_{\theta\theta}^{(1)}\tilde{\sigma}_{rr}^{(1)} + \tilde{\sigma}_{\theta\theta}^{(1)}\tilde{\sigma}_{zz}^{(1)} + \tilde{\sigma}_{rr}^{(1)}\tilde{\sigma}_{zz}^{(1)}) + 2(1+\nu)\tilde{\sigma}_{r\theta}^{(1)2} \right]$$

$$W_2(r, \theta) = \frac{1}{2E} r^{2(\lambda_2-1)} \cdot (K_2^N)^2 \left[ \tilde{\sigma}_{\theta\theta}^{(2)2} + \tilde{\sigma}_{rr}^{(2)2} + \tilde{\sigma}_{zz}^{(2)2} - 2\nu(\tilde{\sigma}_{\theta\theta}^{(2)}\tilde{\sigma}_{rr}^{(2)} + \tilde{\sigma}_{\theta\theta}^{(2)}\tilde{\sigma}_{zz}^{(2)} + \tilde{\sigma}_{rr}^{(2)}\tilde{\sigma}_{zz}^{(2)}) + 2(1+\nu)\tilde{\sigma}_{r\theta}^{(2)2} \right]$$





$$\Delta \bar{W} = \frac{e_1}{E} \left[ \frac{\Delta K_1}{R_0^{1-\lambda_1}} \right]^2 + \frac{e_2}{E} \left[ \frac{\Delta K_2}{R_0^{1-\lambda_2}} \right]^2$$

$R_0$ : control volume radius

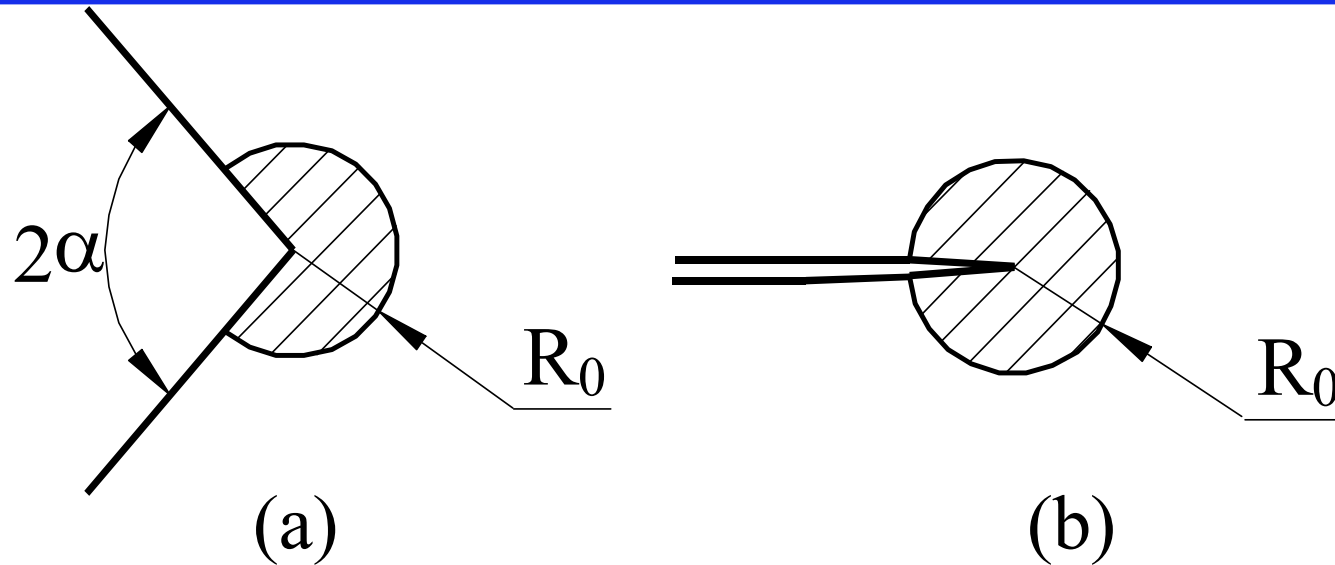
$$e_1 = -5.373 \cdot 10^{-6} (2\alpha)^2 + 6.151 \cdot 10^{-4} (2\alpha) + 0.1330$$

$$e_2 = 4.809 \cdot 10^{-6} (2\alpha)^2 - 2.346 \cdot 10^{-3} (2\alpha) + 0.3400$$

$e_{1,2}$ : shape functions, which depend on the notch angle and Poisson's ratio

$$\Delta \bar{W} = \mathbf{c}_w \left\{ \frac{\mathbf{e}_1}{E} \left[ \frac{\Delta K_1}{R_0^{1-\lambda_1}} \right]^2 + \frac{\mathbf{e}_2}{E} \left[ \frac{\Delta K_2}{R_0^{1-\lambda_2}} \right]^2 + \frac{\mathbf{e}_3}{E} \left[ \frac{\Delta K_3}{R_0^{1-\lambda_3}} \right]^2 \right\}$$

$2\alpha$ [rad]	$\gamma$ [rad]	$\lambda_1$	$\lambda_2$	$\lambda_3$	Plane strain		Axis-sym.
					$\mathbf{e}_1$	$\mathbf{e}_2$	$\mathbf{e}_3$
0	$\pi$	0.5000	0.5000	0.5000	0.13449	0.34139	0.41380
$\pi/12$	$23\pi/24$	0.5002	0.5453	0.5217	0.13996	0.30588	0.39659
$\pi/6$	$11\pi/12$	0.5014	0.5982	0.5455	0.14485	0.27297	0.37929
$\pi/3$	$5\pi/6$	0.5122	0.7309	0.6000	0.15038	0.21530	0.34484
$\pi/2$	$3\pi/4$	0.5445	0.9085	0.6667	0.14623	0.16793	0.31034
$2\pi/3$	$2\pi/3$	0.6157	1.1489	0.7500	0.12964	0.12922	0.27587
$3\pi/4$	$5\pi/8$	0.6736	1.3021	0.8000	0.11721	0.11250	0.25863



$$SED = c_w \times \Delta \overline{W} = \frac{1}{E} \left[ e_1 \times \frac{\Delta K_1^2}{R_1^{2(1-\lambda_1)}} + e_3 \times \frac{\Delta K_3^2}{R_3^{2(1-\lambda_3)}} \right]$$

$$R_1 = \left( \sqrt{2} e_1 \times \frac{\Delta K_{1A}}{\Delta \sigma_{1A}} \right)^{\frac{1}{1-\lambda_1}}$$

$$R_3 = \left( \sqrt{\frac{e_3}{1+\nu}} \times \frac{\Delta K_{3A}}{\Delta \tau_{3A}} \right)^{\frac{1}{1-\lambda_3}}$$

## Advantages

- **Permits consideration of the scale effect**
- **Permits consideration of the contribution of different Modes**
- **Permits consideration of the cycle nominal load ratio**
- **Overcomes the complex problem tied to the different NSIF units of measure in the case of crack initiation at the toe ( $2\alpha=135^\circ$ ) or root ( $2\alpha=0^\circ$ )**
- **SED can be evaluated with coarse meshes**
- **It directly takes into account the T-stress**
- **It directly includes three-dimensional effects**
- **Direct link with other local approaches (NSIFs, PS method, critical distances)**
- **Not specific coefficient to be set up**





## Tests

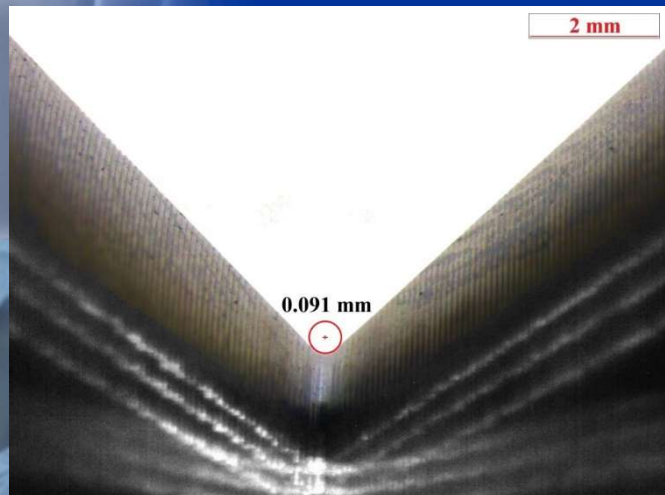
Analysis of the bi-axial fatigue behaviour of notched specimens in Ti6Al4V (Gr. 5) alloy under combined tensile and torsion loading, both in-phase and out-of-phase, with particular reference to the evaluation of HCF

Application of an energy-based approach to summarise the fatigue data in presence of severe notches

- Tensile fatigue tests on notched specimens ( $R=-1$  and  $R=0$ ,  $f=5-20$  Hz)
- Torsional fatigue tests on notched specimens ( $R=-1$  and  $R=0$ ,  $f=5-20$  Hz)
- Combined tensile-torsional fatigue tests on notched specimens
- Analysis of the influence of load ratio on the multiaxial fatigue behaviour ( $R=0$  and  $R=-1$ ,  $f=5-20$  Hz)
- Analysis of the influence of biaxiality ratio on the multiaxial fatigue behaviour ( $\lambda=0.6$  and  $2$ ,  $f=5-20$  Hz)
- Analysis of the influence of the phase angle on the multiaxial fatigue behaviour ( $\Phi=0$  and  $\Phi=90^\circ$ ,  $f=5-20$  Hz)

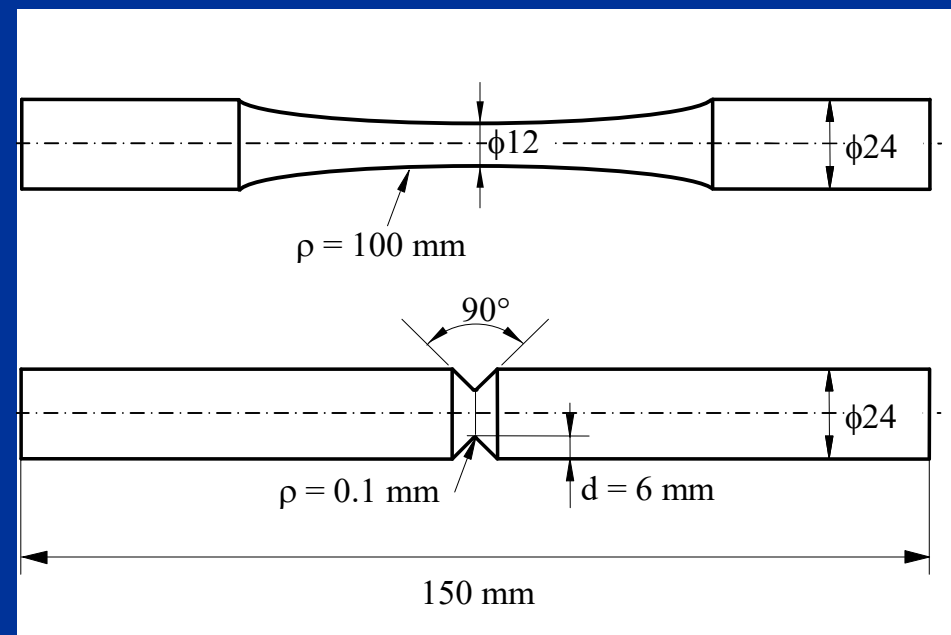
# MATERIAL: Ti6Al4V

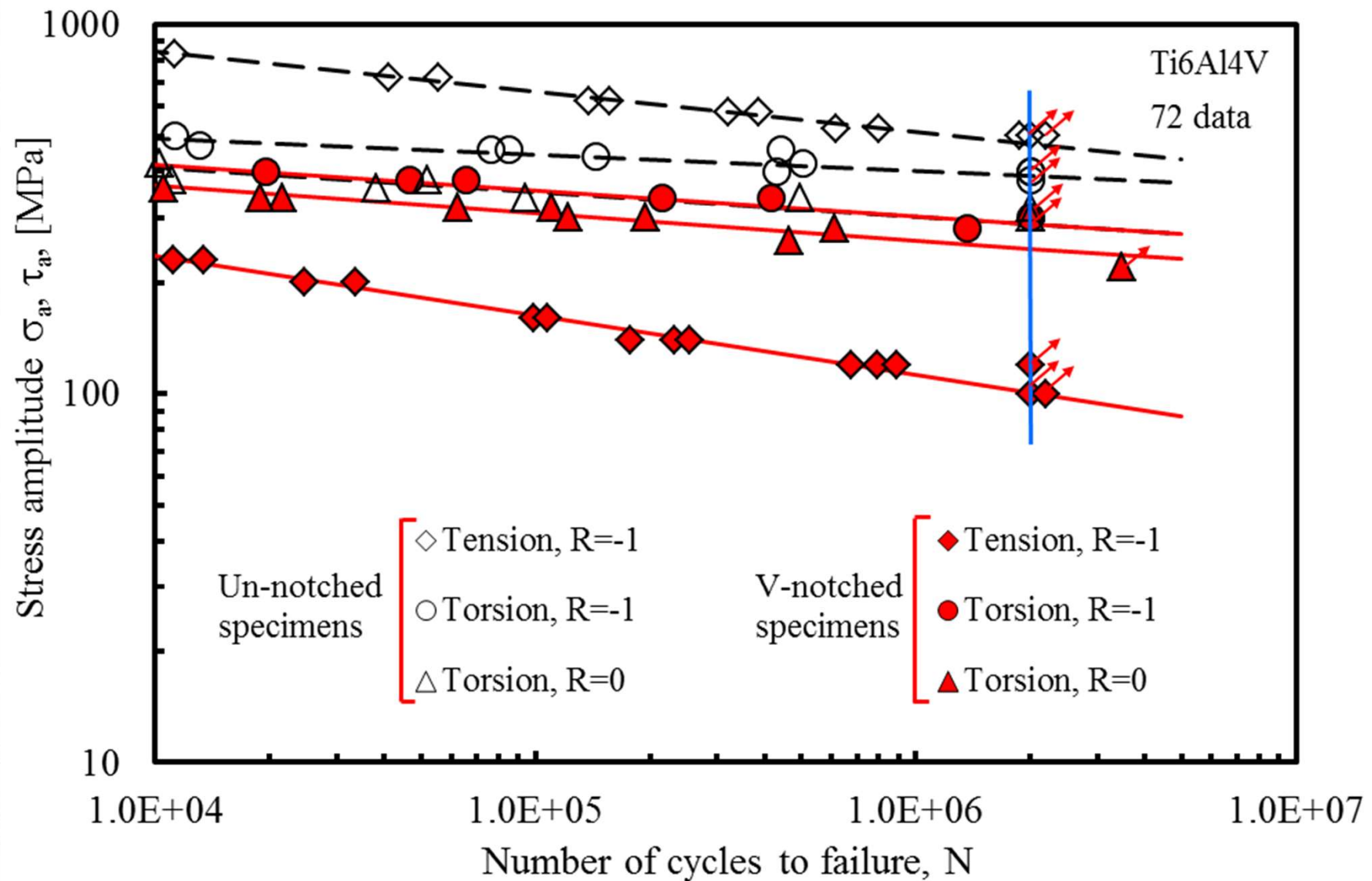
$E = 110 \text{ GPa}$ ,  $\sigma_{\text{uts}} = 995 \text{ MPa}$ ,  $\sigma_y = 880 \text{ MPa}$

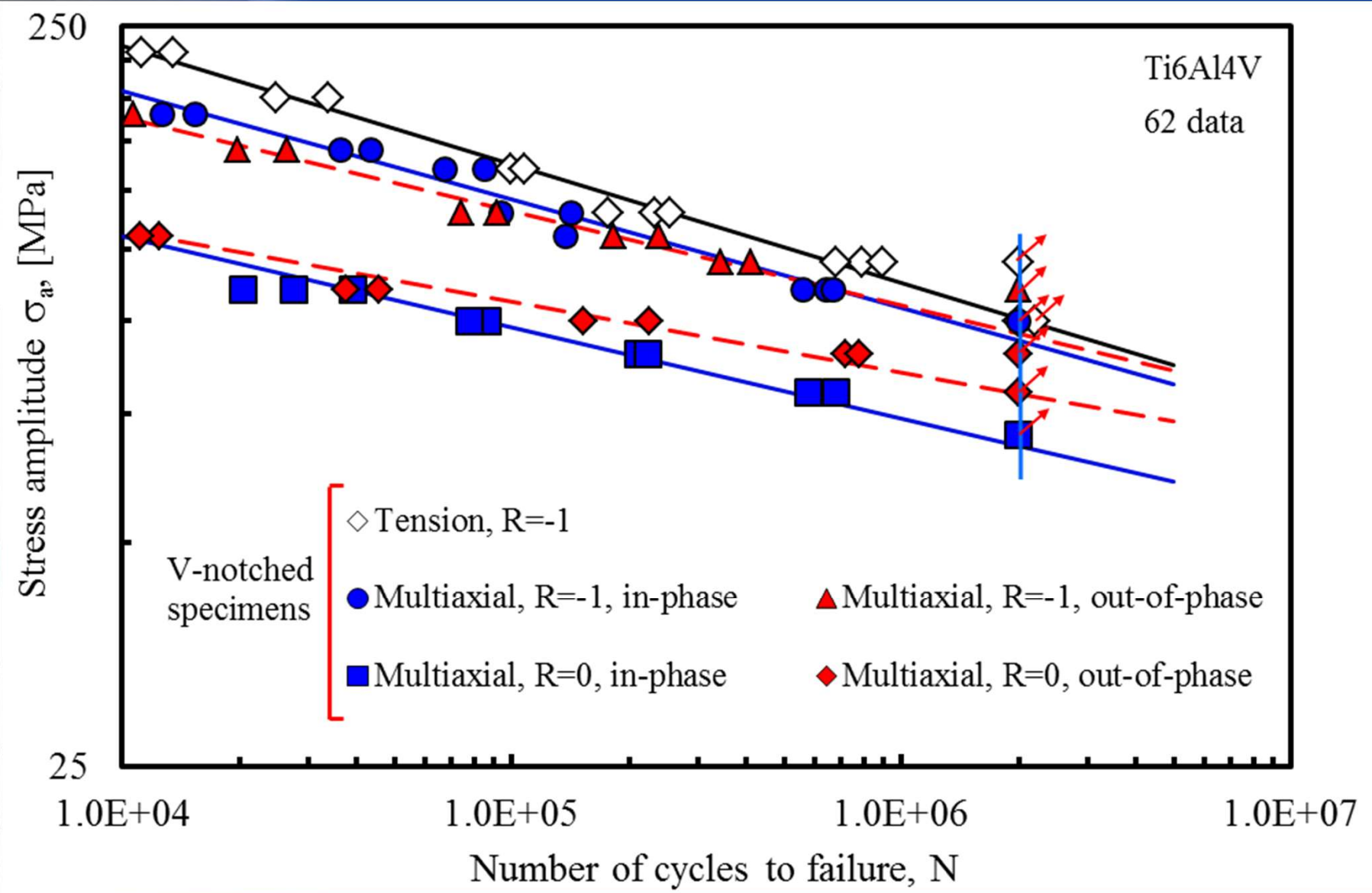


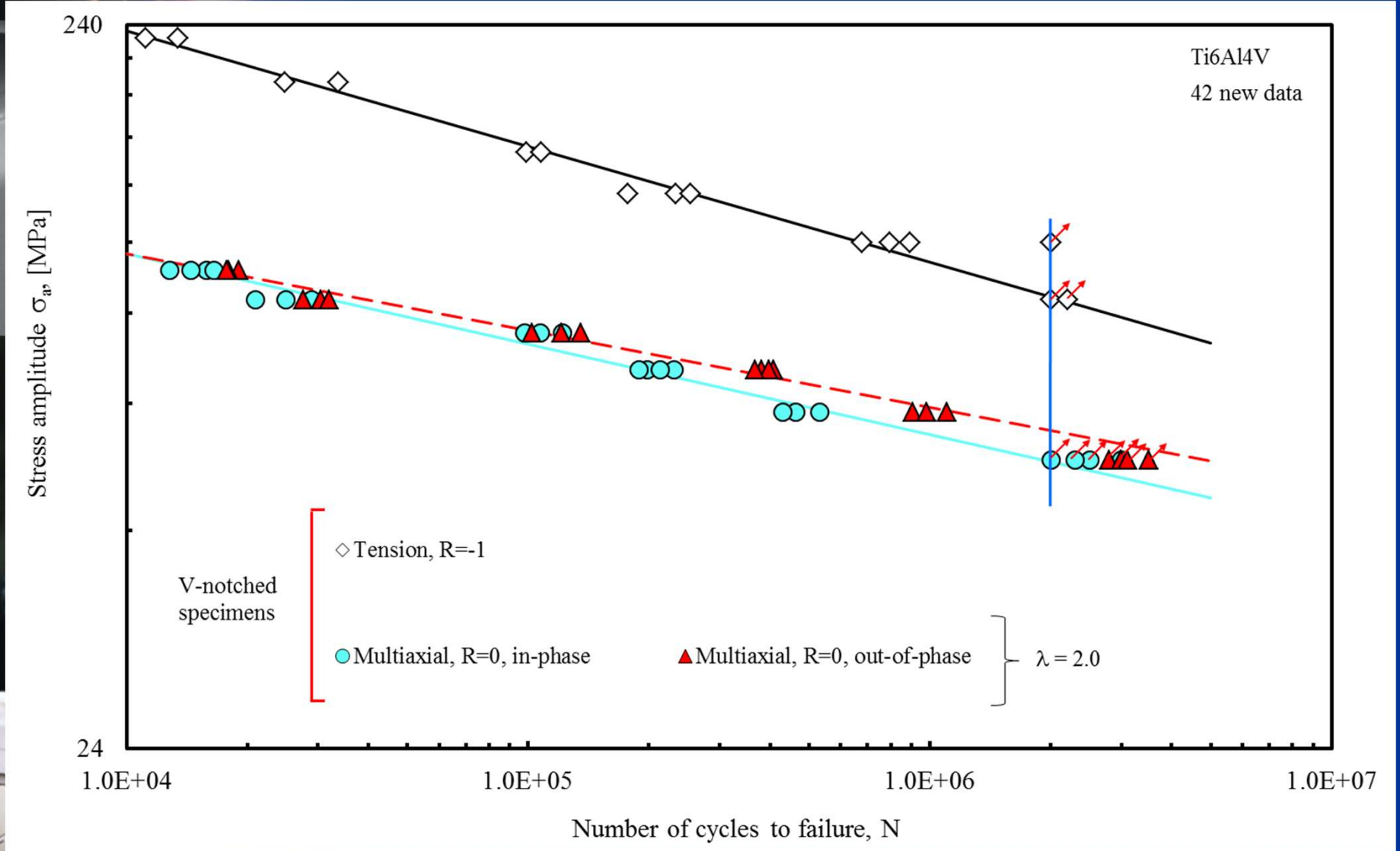
**Unnotched specimens**

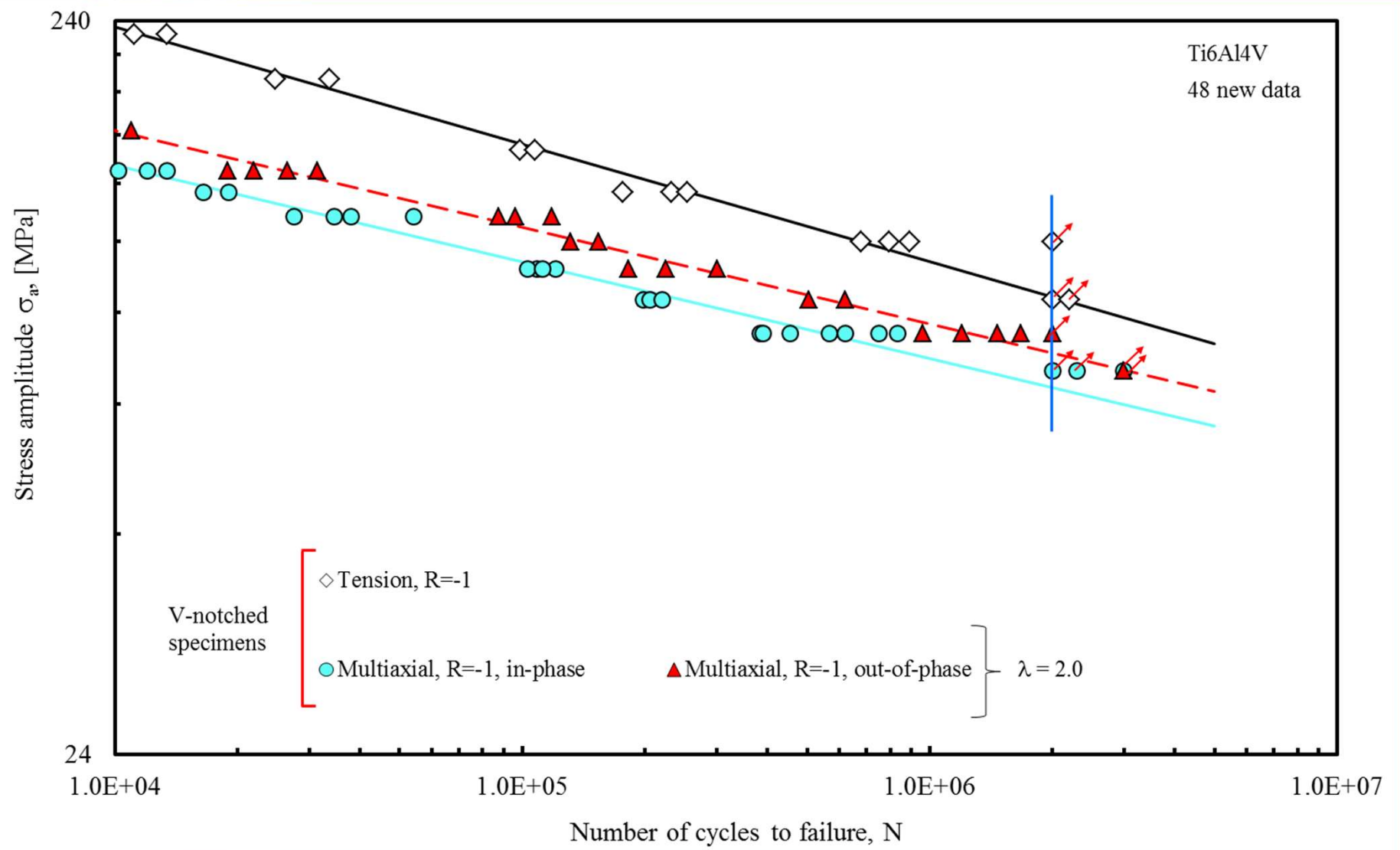
**Notched specimens with  $\rho < 0.1 \text{ mm}$**

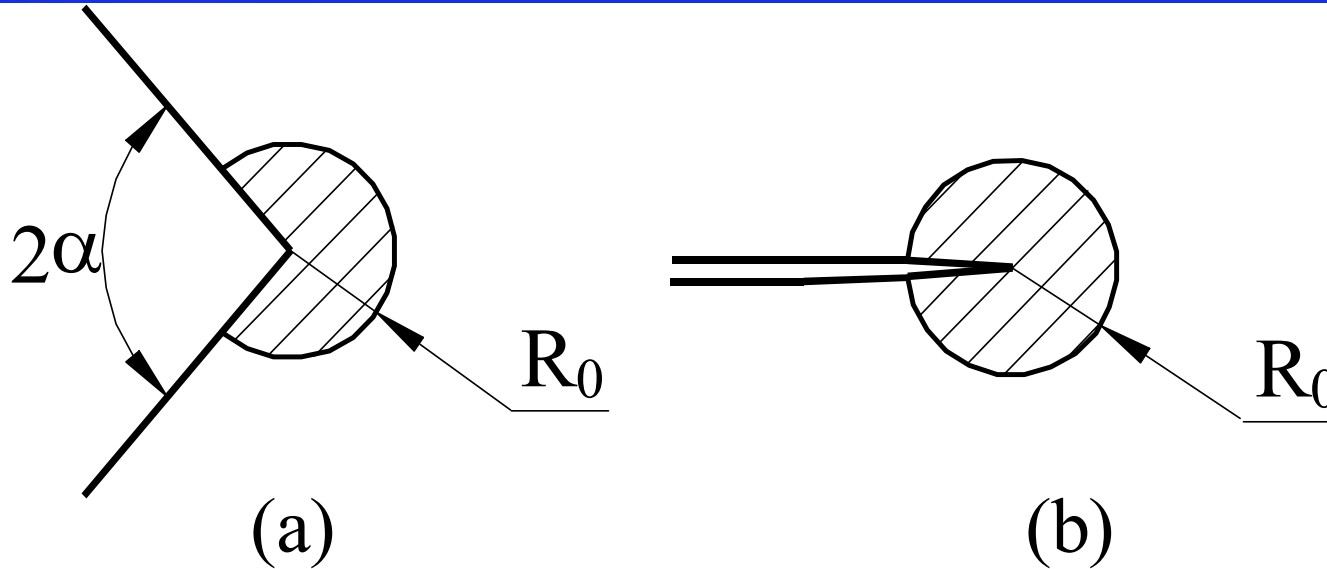












$$SED = c_W \times \Delta \bar{W} = \frac{1}{E} \left[ e_1 \times \frac{\Delta K_1^2}{R_1^{2(1-\lambda_1)}} + e_3 \times \frac{\Delta K_3^2}{R_3^{2(1-\lambda_3)}} \right]$$

$$R_1 = \left( \sqrt{2} e_1 \times \frac{\Delta K_{1A}}{\Delta \sigma_{1A}} \right)^{\frac{1}{1-\lambda_1}}$$

$$R_3 = \left( \sqrt{\frac{e_3}{1+\nu}} \times \frac{\Delta K_{3A}}{\Delta \tau_{3A}} \right)^{\frac{1}{1-\lambda_3}}$$

- Plain (unnotched specimens): Beltrami's expressions

Pure tension  $\Delta\bar{W} = c_w \frac{\Delta\sigma_{\text{nom}}^2}{2E}$

Pure Torsion  $\Delta\bar{W} = c_w(1 + \nu) \frac{\Delta\tau_{\text{nom}}^2}{E}$

- V-notched specimens: SED in a control volume

$$\Delta\bar{W} = \frac{c_w}{E} \left[ e_1 \cdot \frac{\Delta K_1^2}{R_1^{2(1-\lambda_1)}} + e_3 \cdot \frac{\Delta K_3^2}{R_3^{2(1-\lambda_3)}} \right]$$



$$R_1 = \left( \sqrt{2} e_1 \times \frac{\Delta K_{1A}}{\Delta \sigma_{1A}} \right)^{\frac{1}{1-\lambda_1}}$$

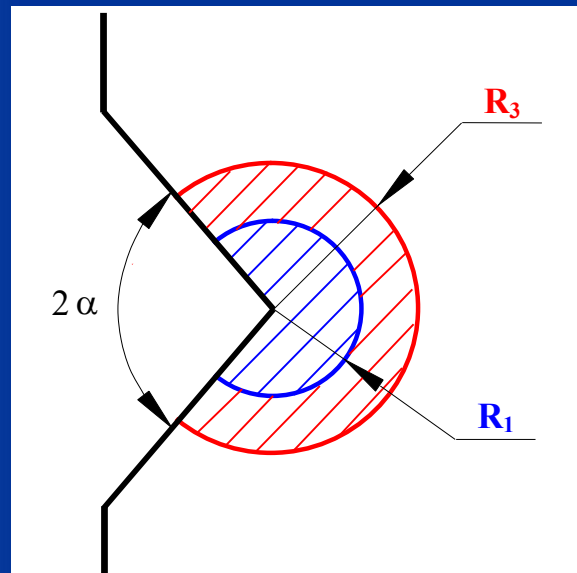
$$R_3 = \left( \sqrt{\frac{e_3}{1+\nu}} \times \frac{\Delta K_{3A}}{\Delta \tau_{3A}} \right)^{\frac{1}{1-\lambda_3}}$$

**For mode 1 loading:**

$$\Delta K_{1A} = 452 \text{ MPa}\cdot\text{mm}^{0.455} ; \Delta \sigma_{1A} = 950 \text{ MPa}$$

**For mode 3 loading:**

$$\Delta K_{3A} = 1216 \text{ MPa}\cdot\text{mm}^{0.333} ; \Delta \tau_{3A} = 776 \text{ MPa}$$



$$R_1 = 0.051 \text{ mm}$$

$$R_3 = 0.837 \text{ mm}$$

# STRAIN ENERGY DENSITY AT THE NOTCH TIP

## MODE 1 + MODE 3

- $\Delta K_1$  and  $\Delta K_3$  are the NSIFs range under Mode I and Mode III:

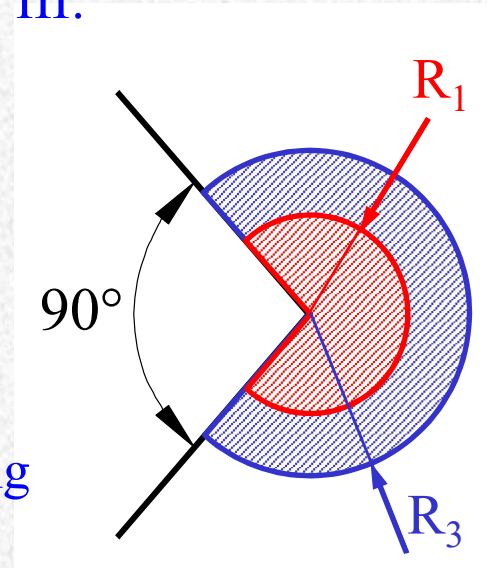
$$\Delta K_1 = k_1 d^{1-\lambda_1} \Delta \sigma_{\text{nom}} = 2.260 \Delta \sigma_{\text{nom}} \quad (\text{MPa mm}^{0.445})$$

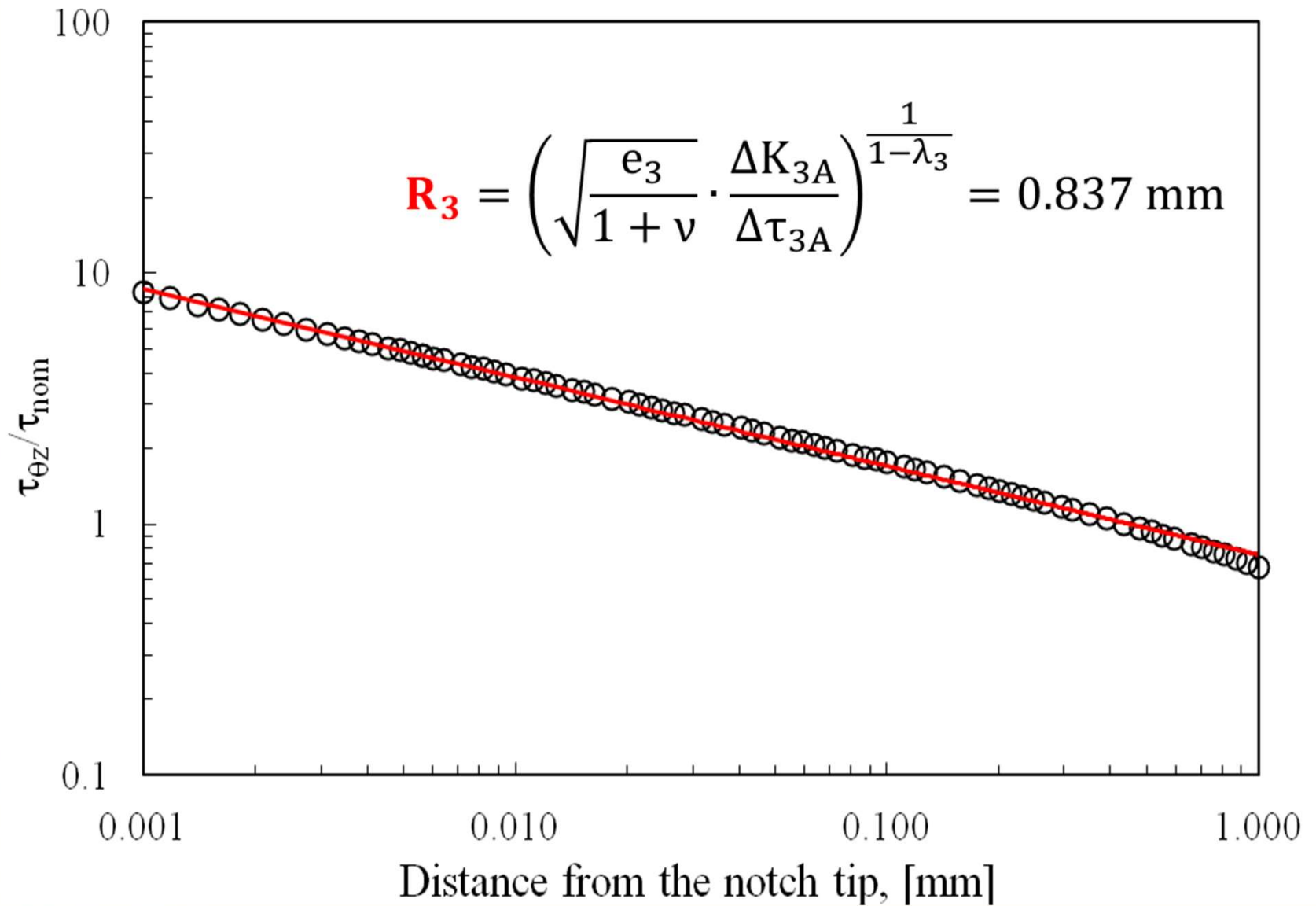
$$\Delta K_3 = k_3 d^{1-\lambda_3} \Delta \tau_{\text{nom}} = 2.096 \Delta \tau_{\text{nom}} \quad (\text{MPa mm}^{0.333})$$

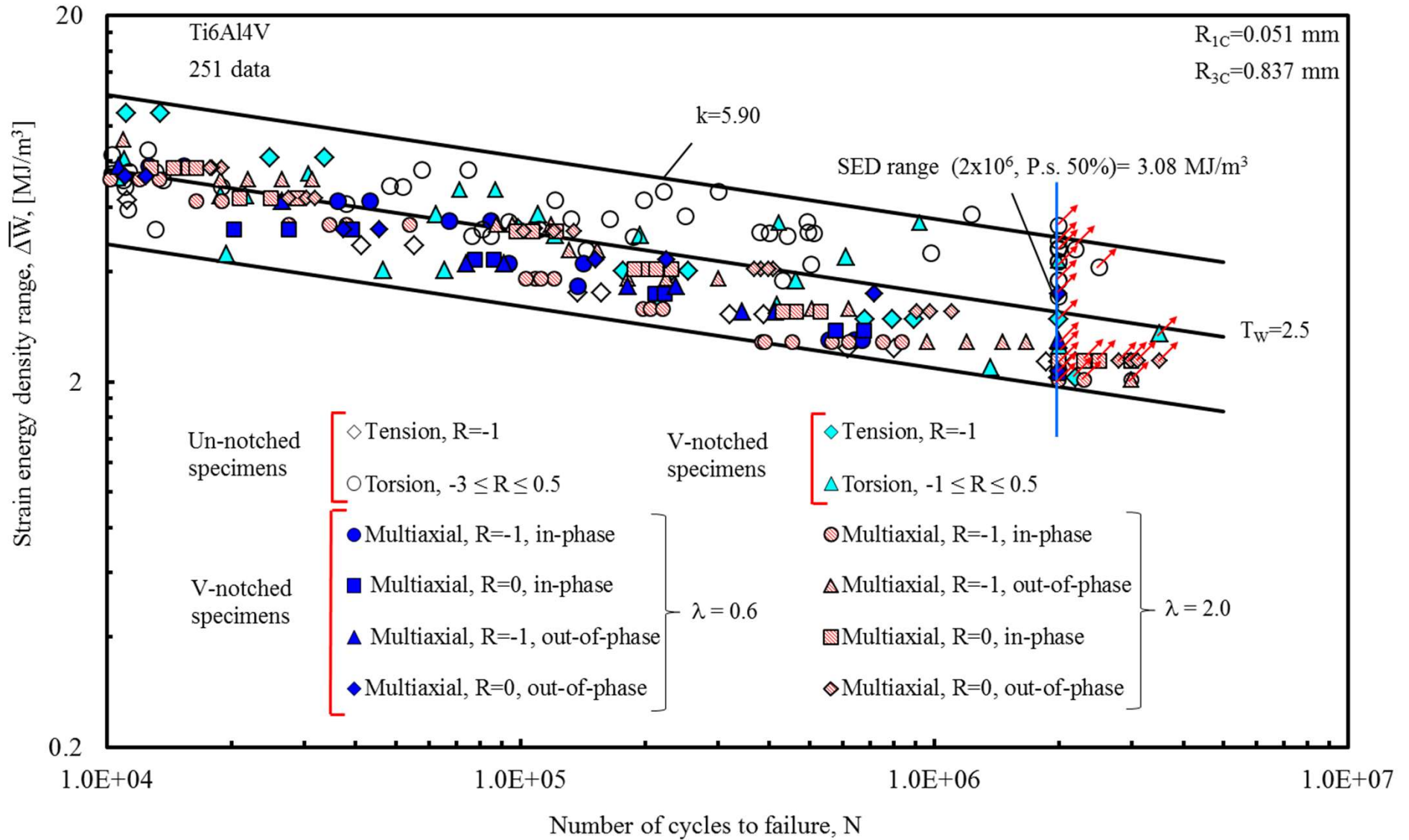
- $e_1 = 0.146$  and  $e_3 = 0.310$  depend on the notch opening angle and Poisson's ratio;

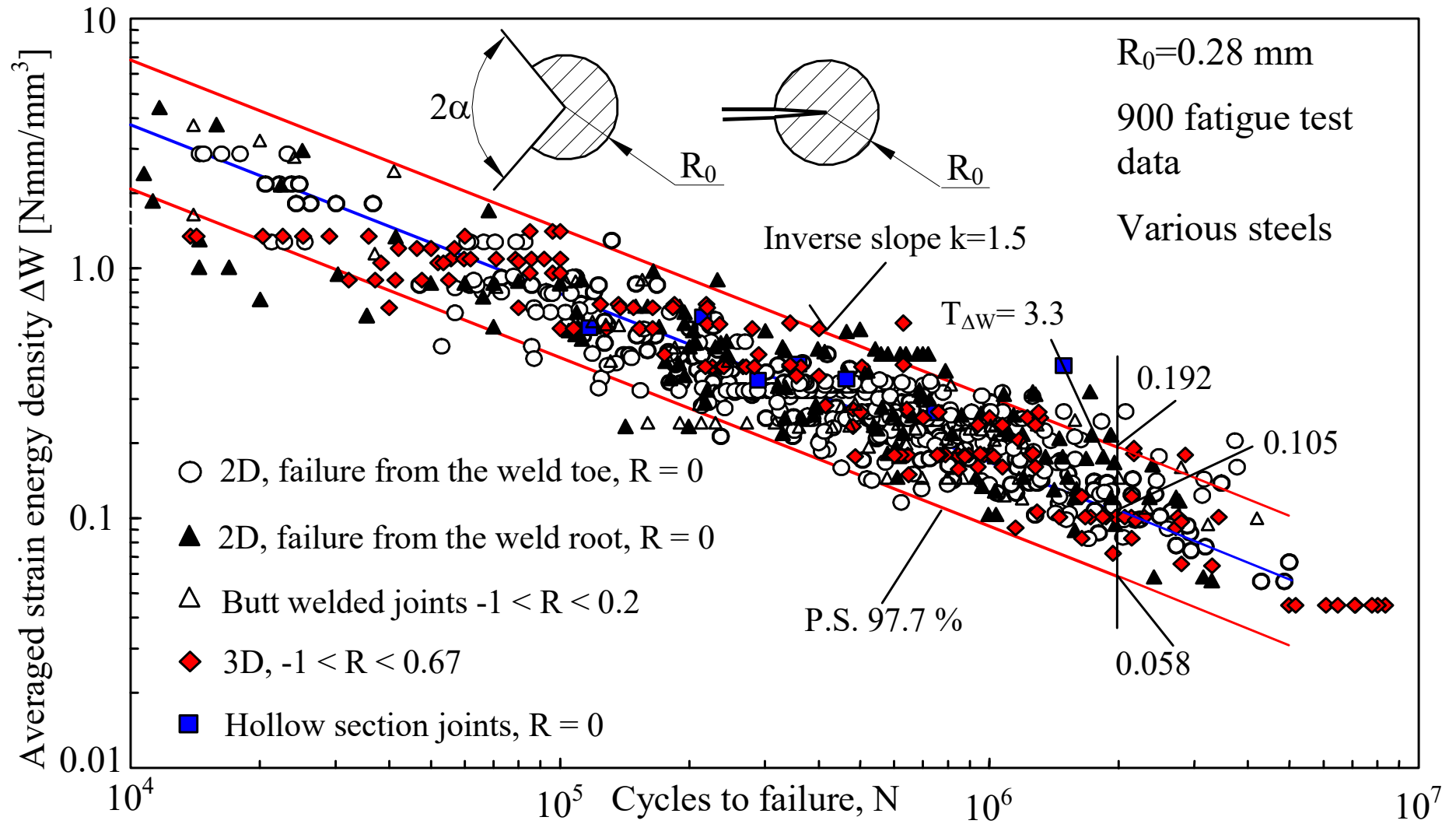
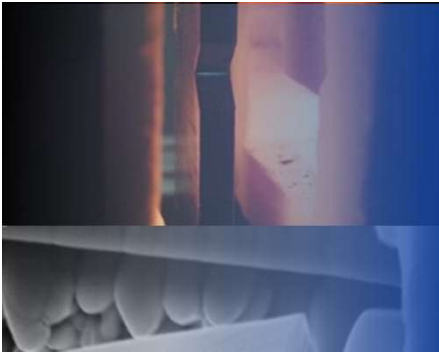
- The control radii depend on the fatigue strength of unnotched specimens and on the stress range of the NSIFs values:

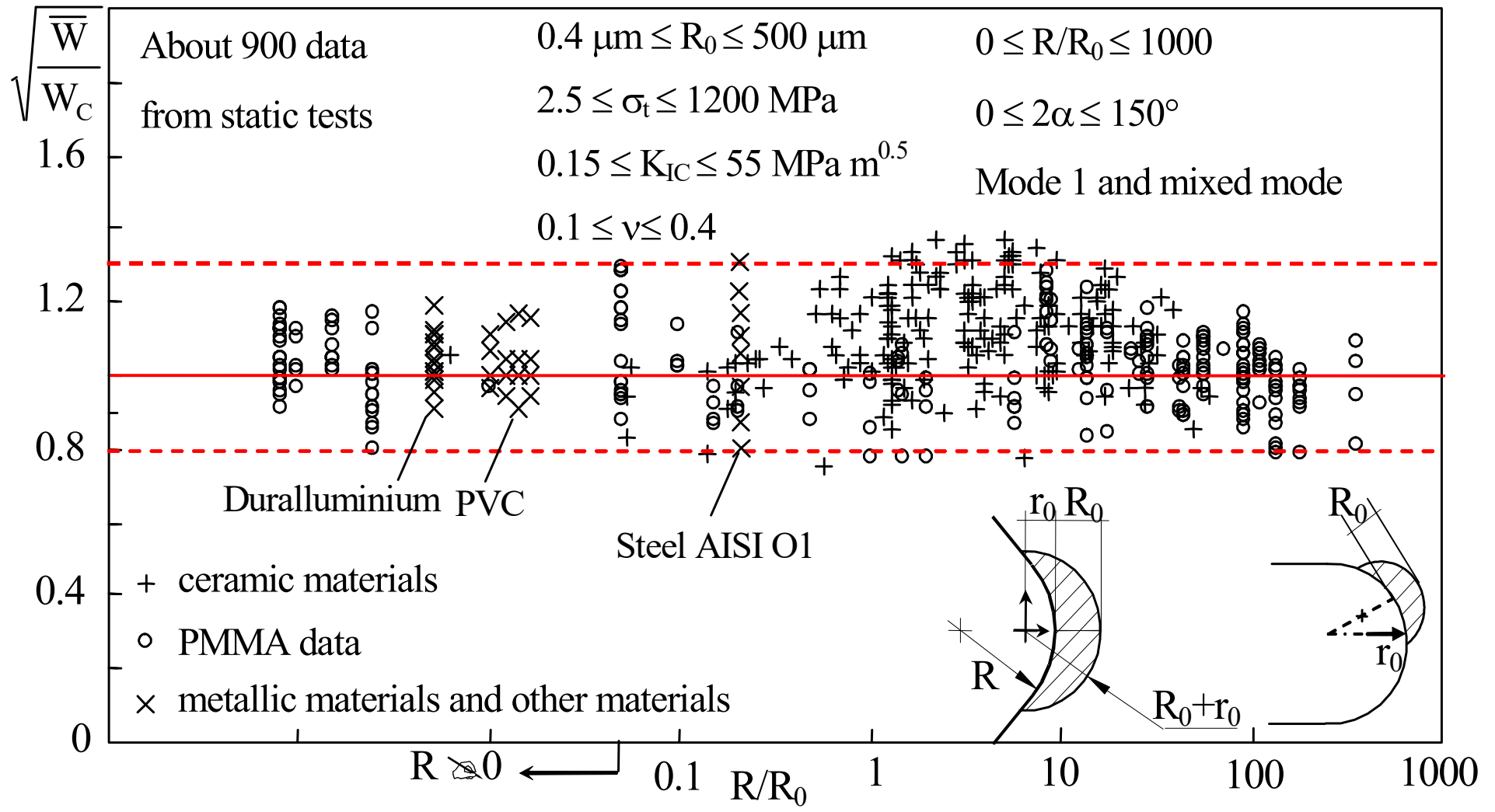
$$\mathbf{R}_1 = \left( \sqrt{2e_1} \cdot \frac{\Delta K_{1A}}{\Delta \sigma_{1A}} \right)^{\frac{1}{1-\lambda_1}} = 0.051 \text{ mm} \quad \mathbf{R}_3 = \left( \sqrt{\frac{e_3}{1+\nu}} \cdot \frac{\Delta K_{3A}}{\Delta \tau_{3A}} \right)^{\frac{1}{1-\lambda_3}} = 0.837 \text{ mm}$$



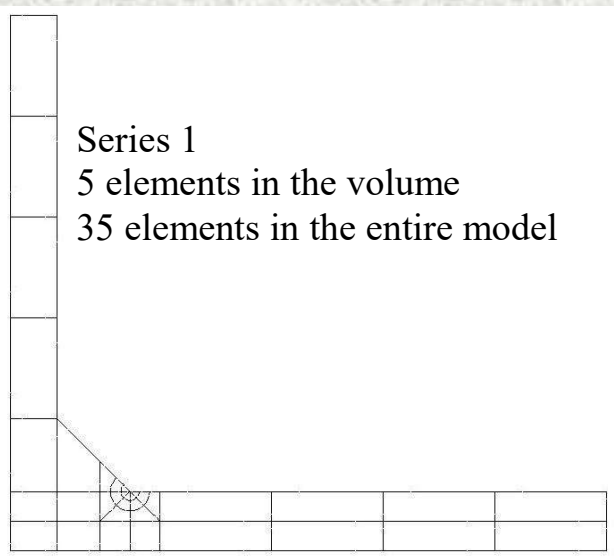
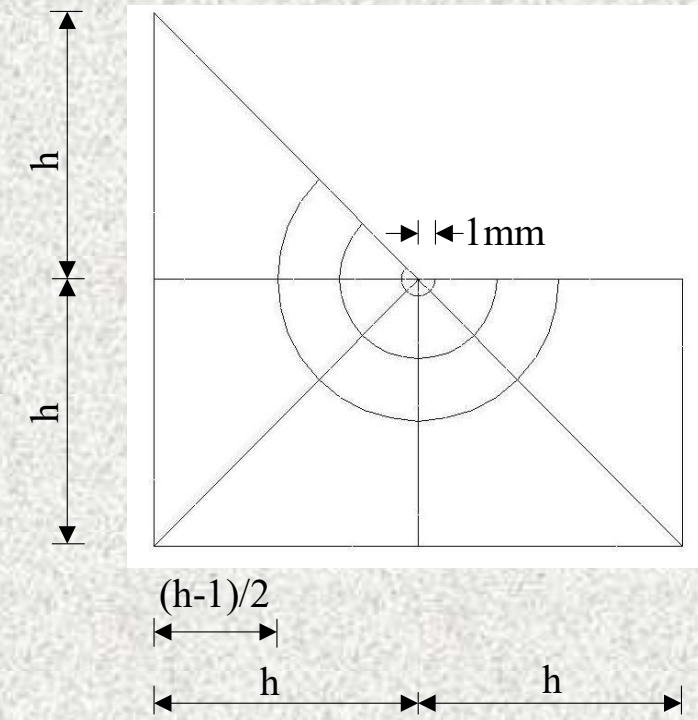
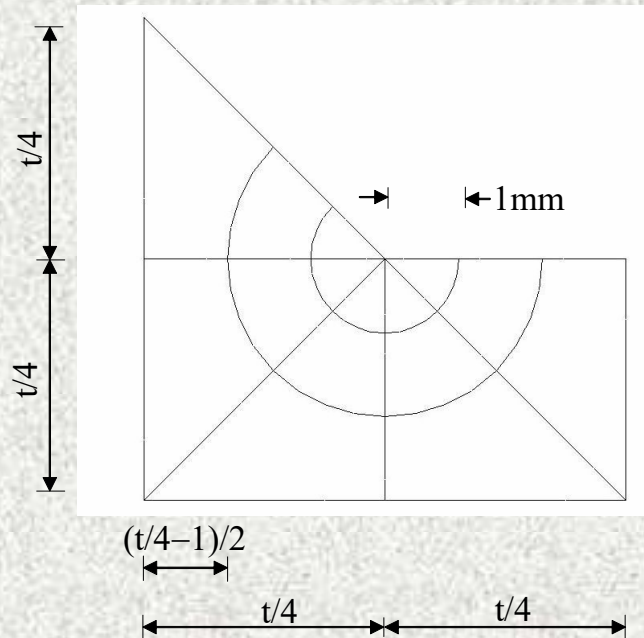






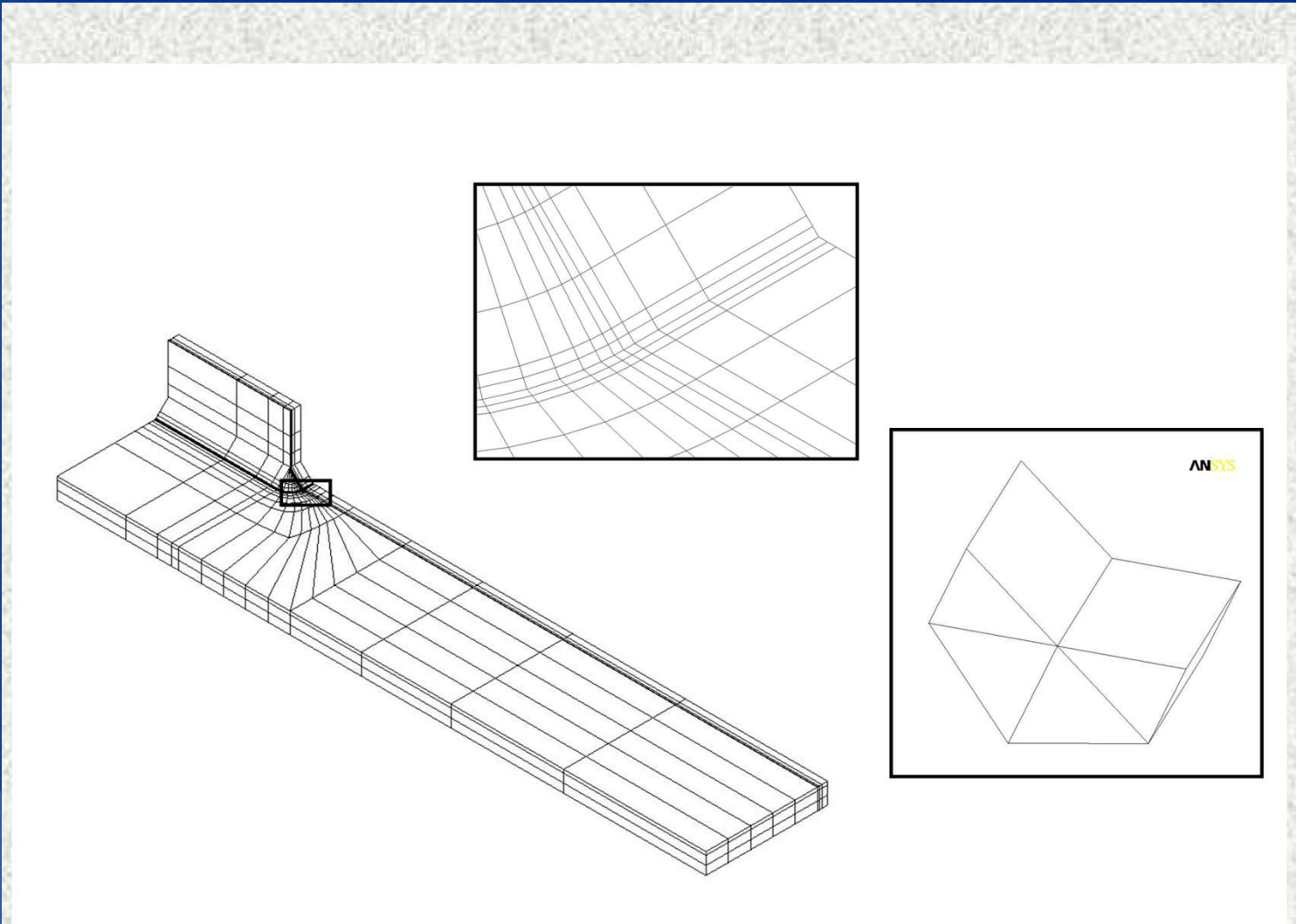


# Coarse mesh



3/01/2018

# Coarse mesh

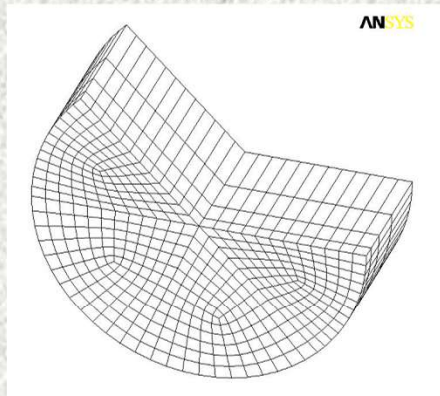




# Coarse mesh

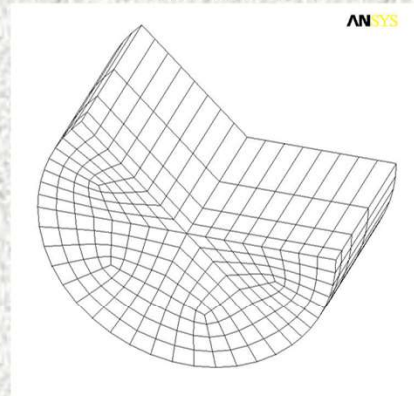


**Mesh 1**



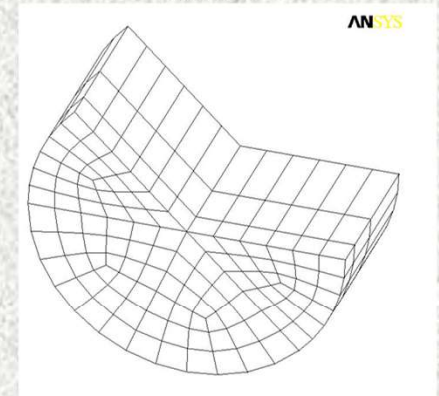
1969 elements

**Mesh 2**



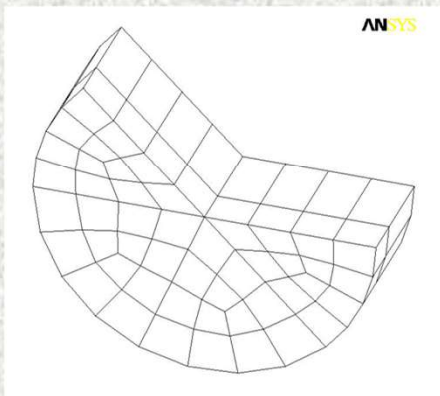
768 elements

**Mesh 3**



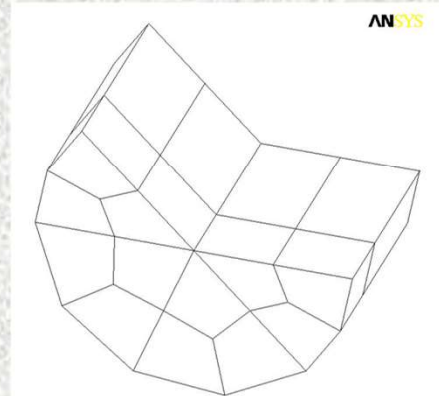
324 elements

**Mesh 4**



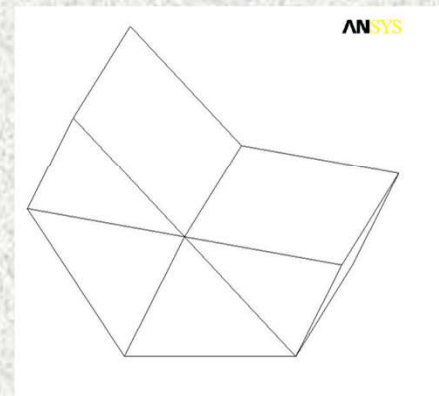
96 elements

**Mesh 5**



24 elements

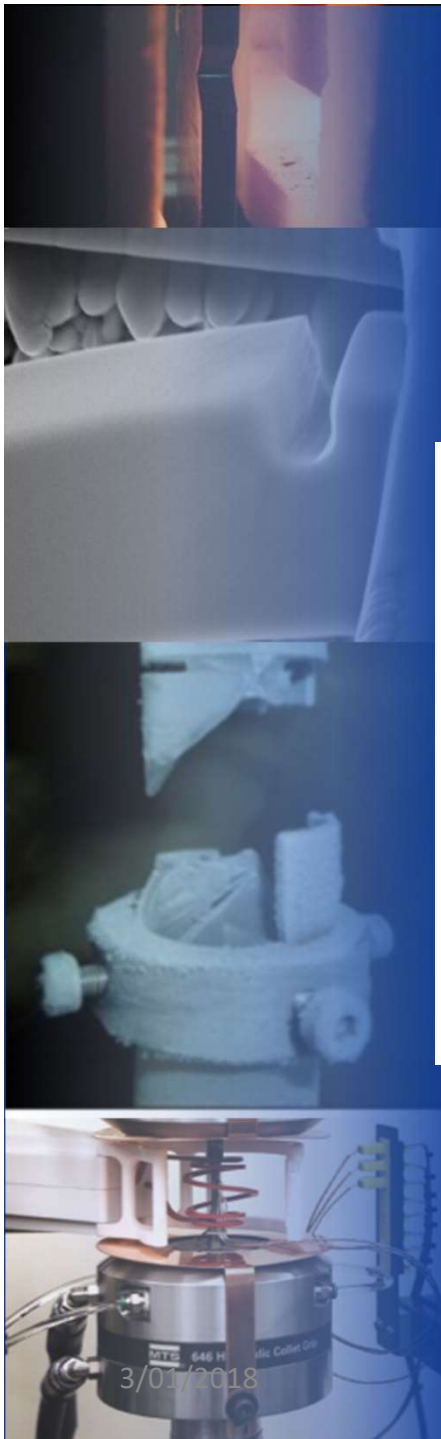
**Mesh 6**



4 elements

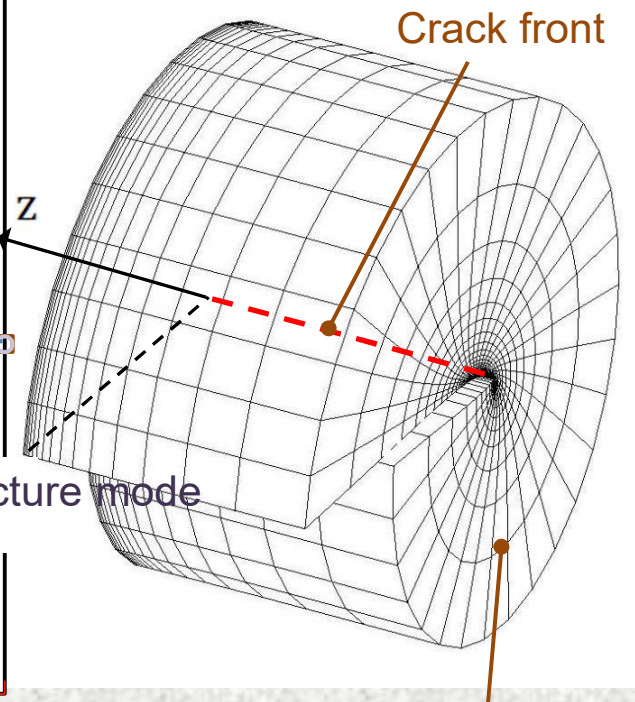
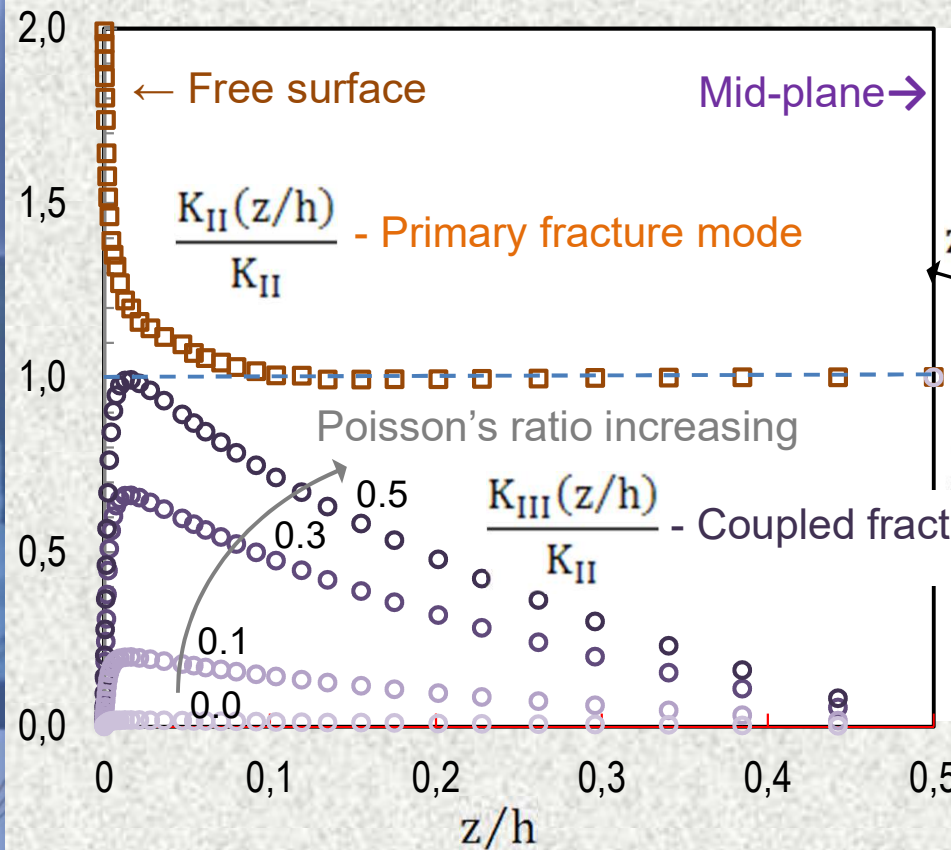
# Coarse mesh

3D models	Number of FE in the volume	Degrees of freedom (complete model)	$\bar{W}$ Nmm/mm <sup>3</sup>	$K_1$ [MPa mm <sup>0.326</sup> ]	$\Delta\%$
1	1696	$8.6 \cdot 10^5$	0.07937	373.5	0
2	768	$4.6 \cdot 10^5$	0.07903	372.7	0.21
3	324	$2.5 \cdot 10^5$	0.07896	372.5	0.26
4	96	$1.7 \cdot 10^5$	0.07895	372.5	0.26
5	24	$4.5 \cdot 10^4$	0.07790	370.0	0.93
6	4	$1.1 \cdot 10^4$	0.07594	365.3	2.18



3/01/2018

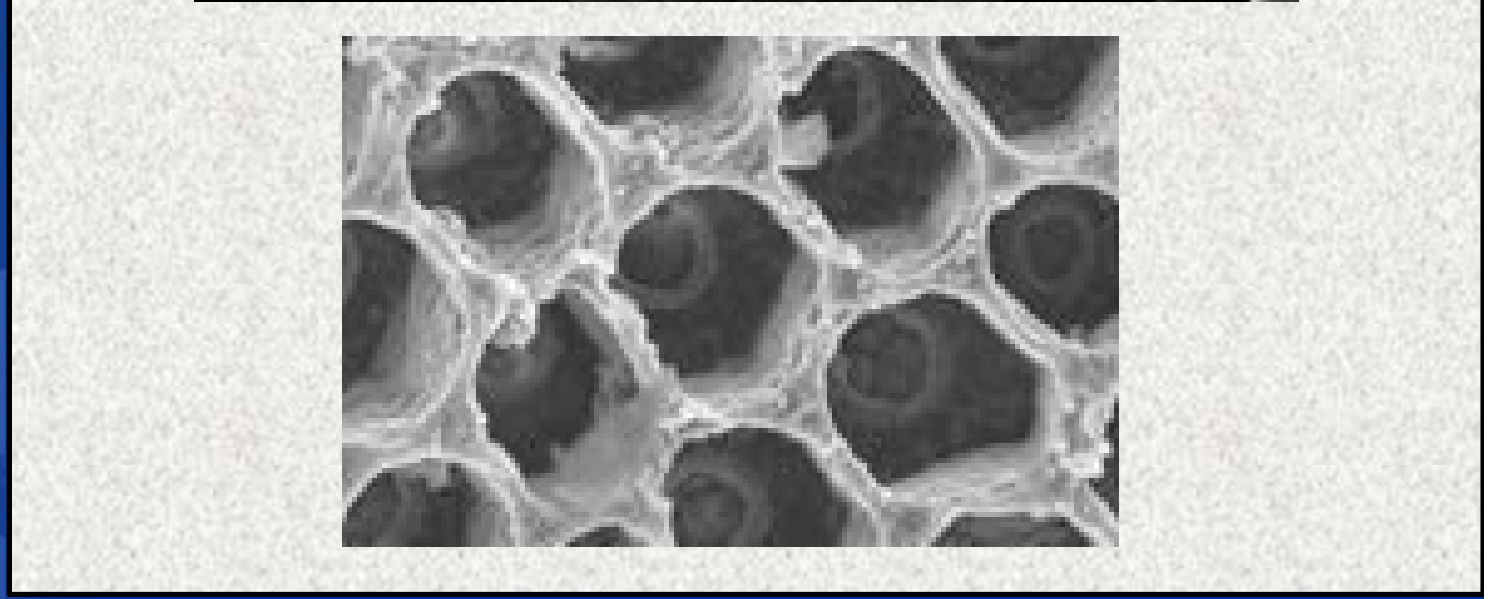
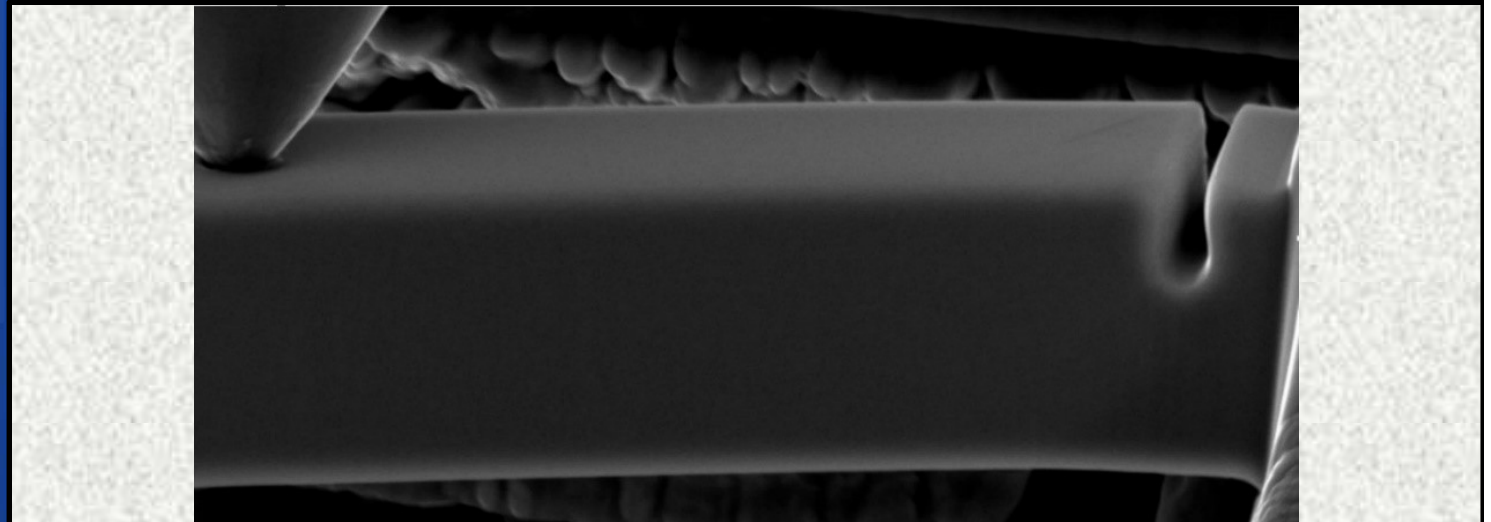
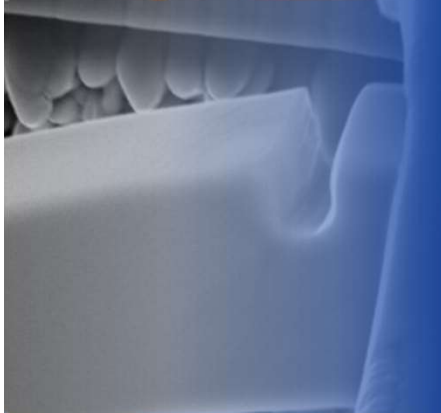
# Coupled Fracture Modes



**Mechanism of generation of coupled mode: Poisson's Effect**



# Nanoscale (1)



# Nanoscale (2)

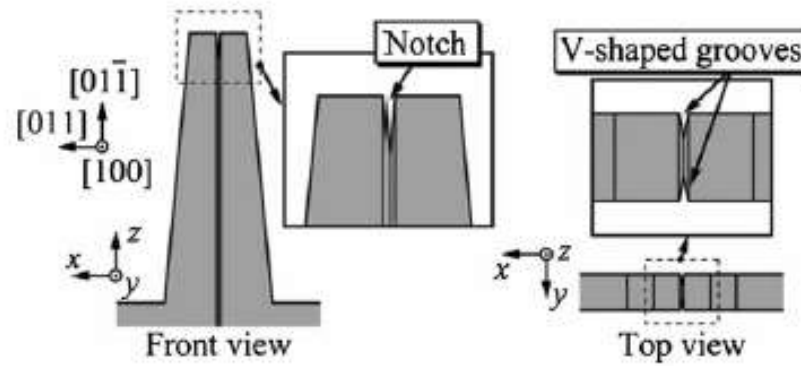


Fig. 1 Si specimen with notch.

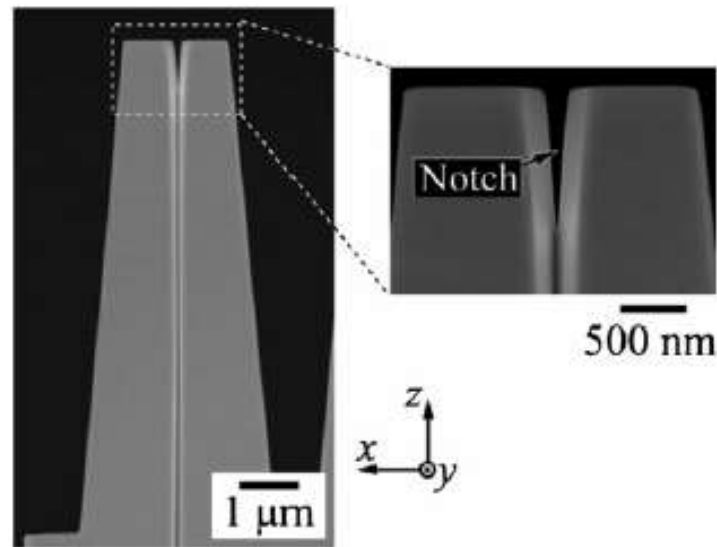
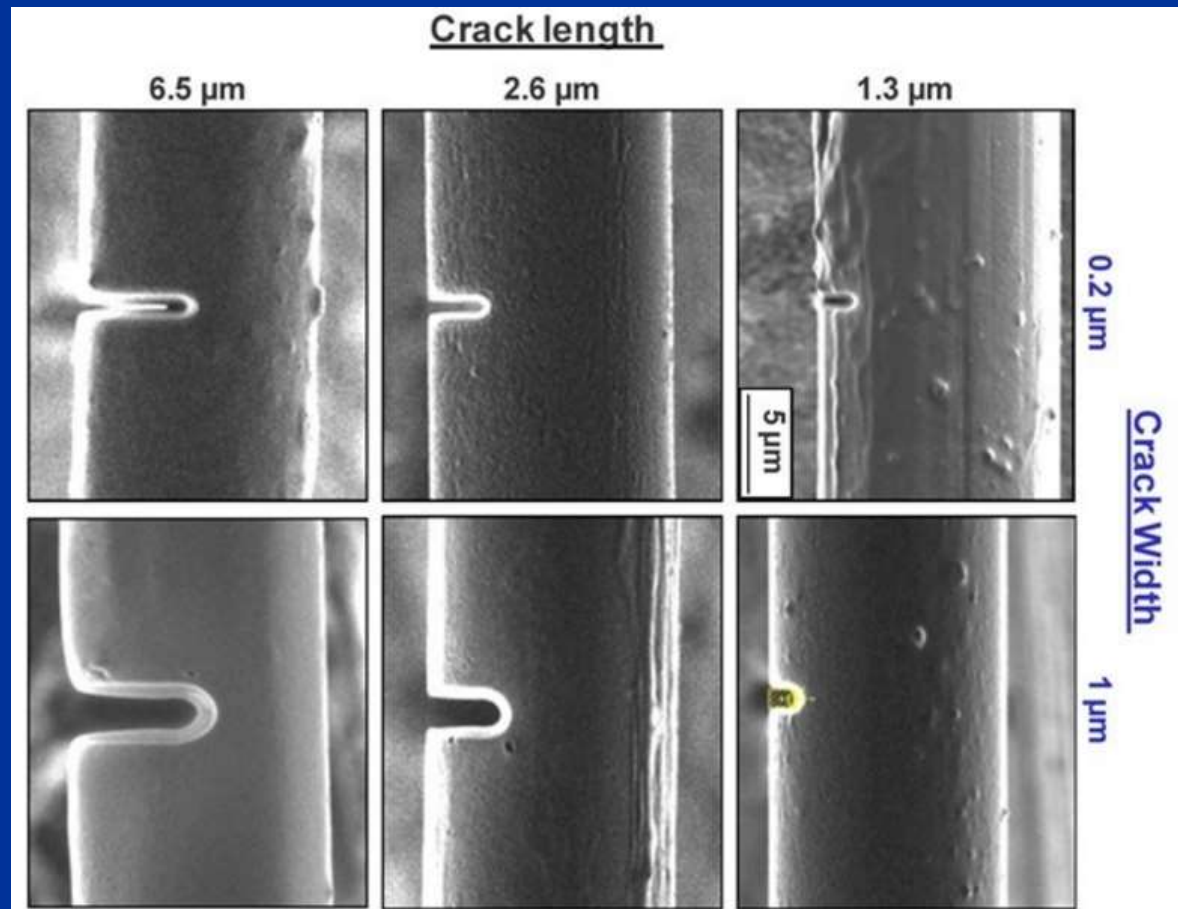
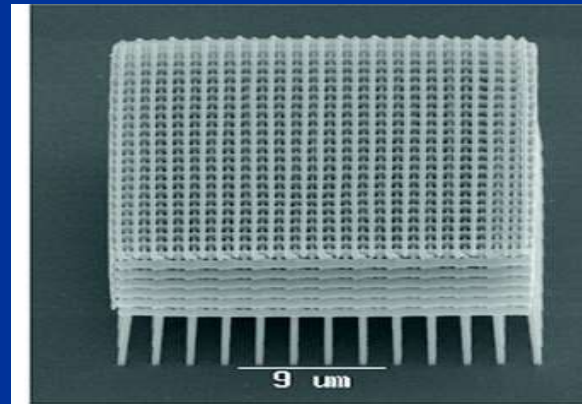


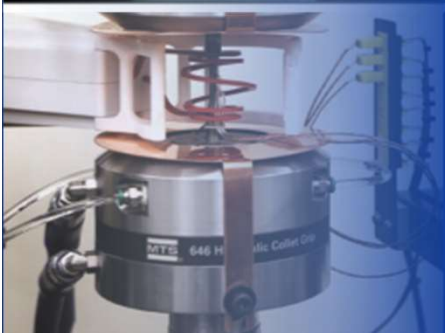
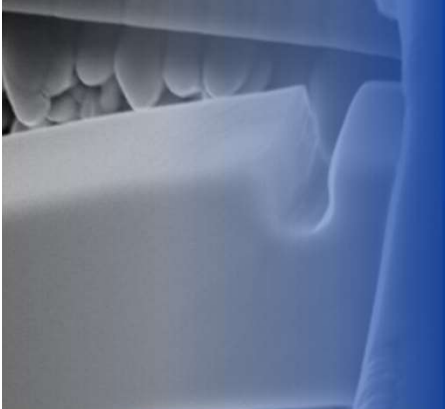
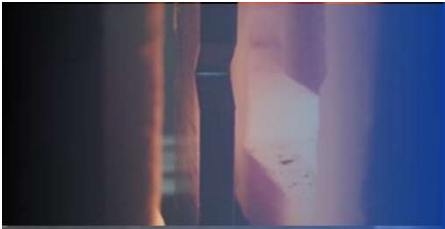
Fig. 2 Scanning electron microscopy image of the specimen with notch.



# Microscale



# Intermediate scale



# Additive Materials



Department of Mechanical Engineering



**Additive Manufacturing (AM) materials under fatigue loading from full scale to nano level.**

**Examination of the state-of-the-art shows that fatigue assessment and quality assurance of additively manufactured components cannot be performed accurately due to a lack of bespoke methodologies allowing the specific microstructural features as well as the specific mechanical/cracking behaviour of additively manufactured materials to be modelled effectively.**





# Additive Materials



**Topological complexity**



**Material/Hierarchical complexity**



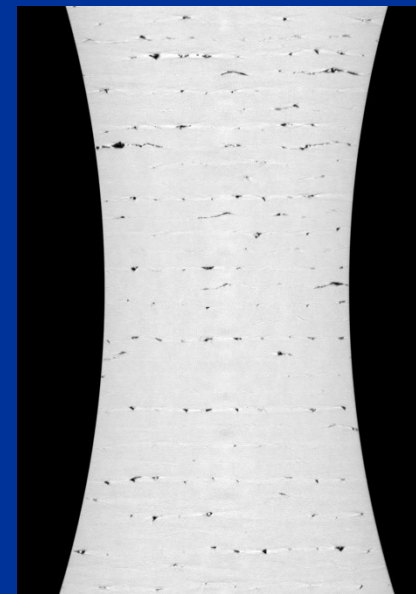
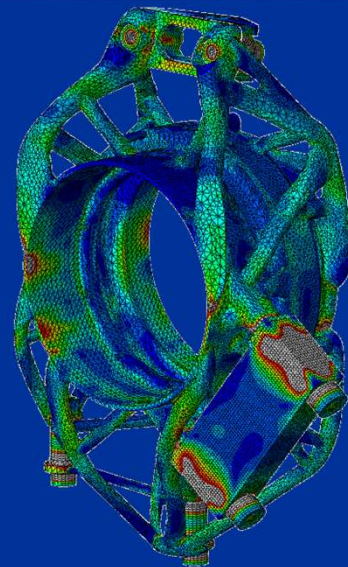
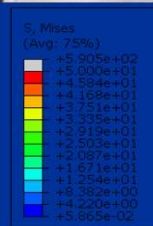
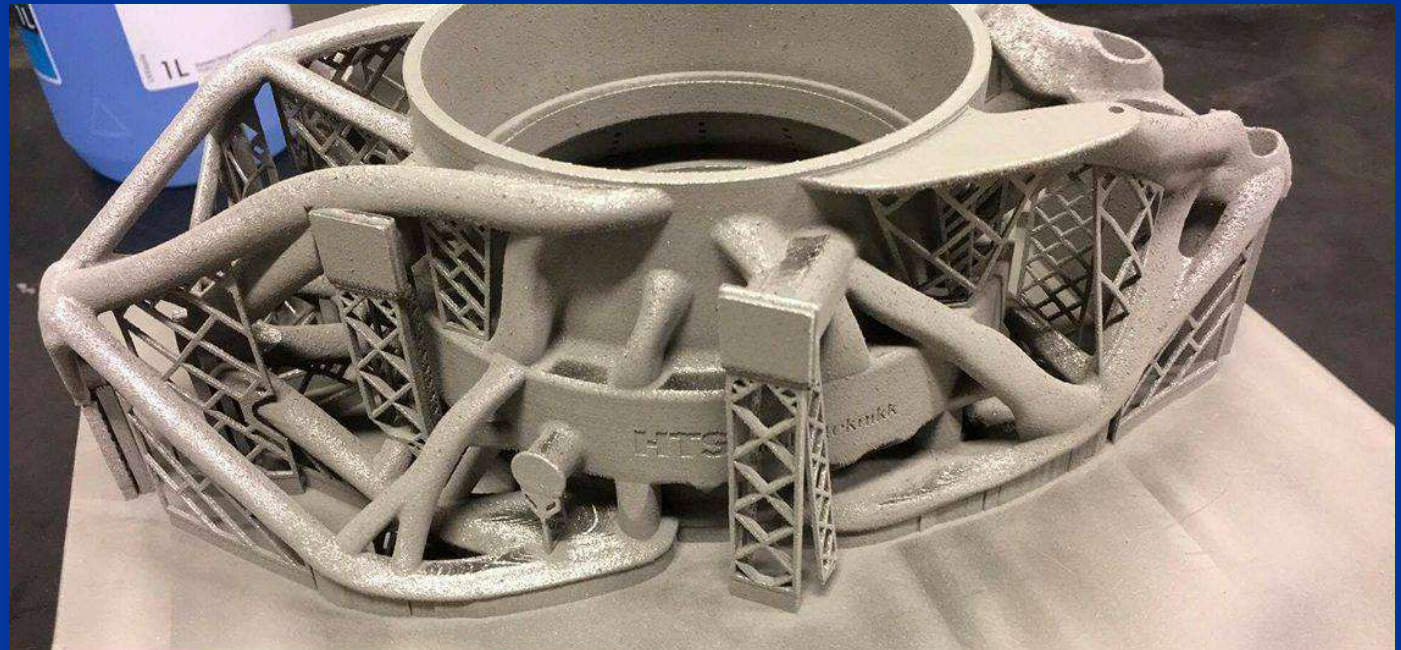
**Functional complexity**

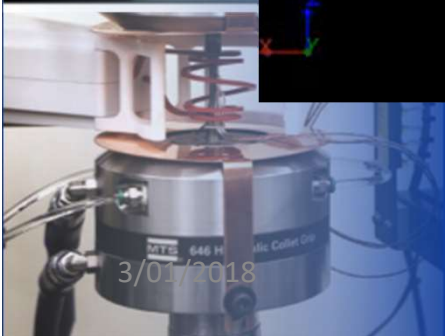


**Quality assurance**

# Additive Materials

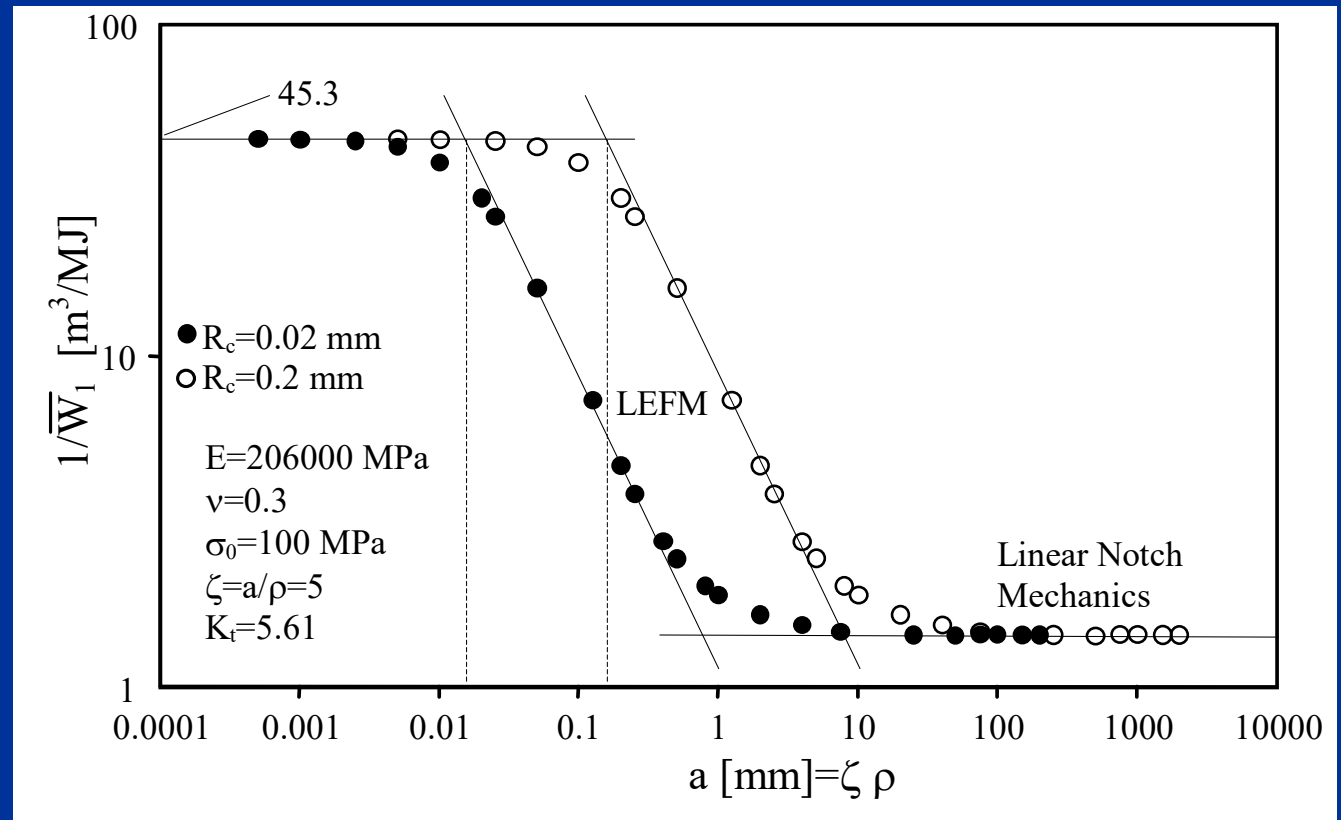
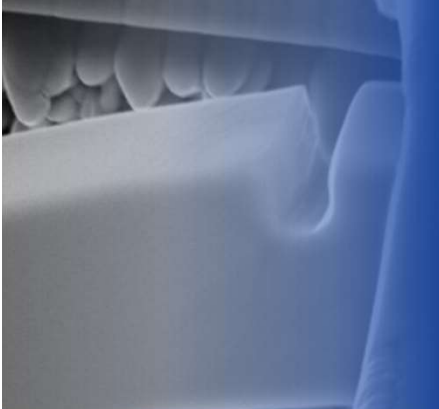
## Interactions btw notches and defects





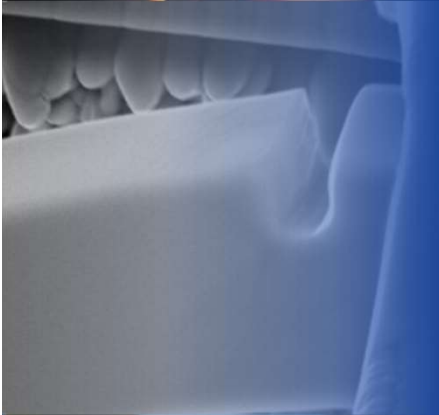
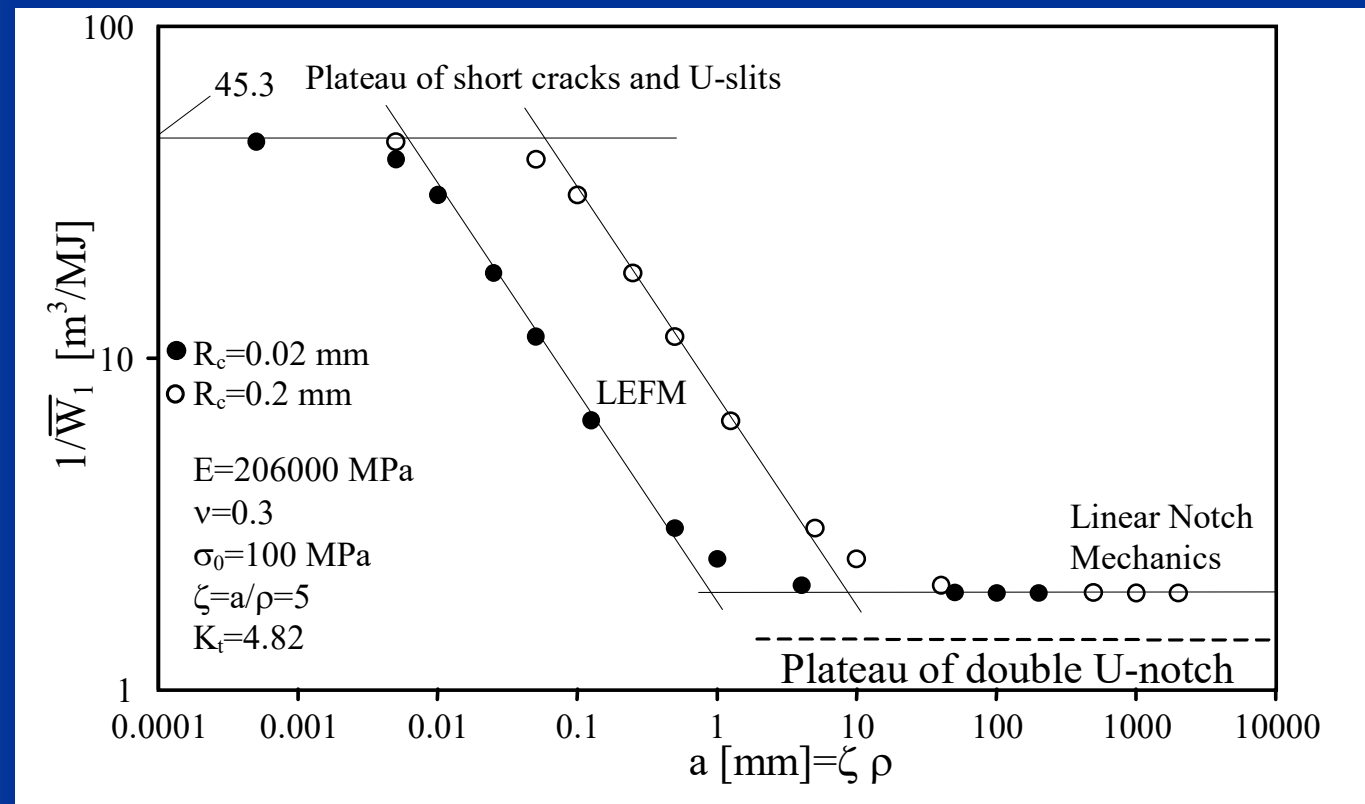
# Additive Materials

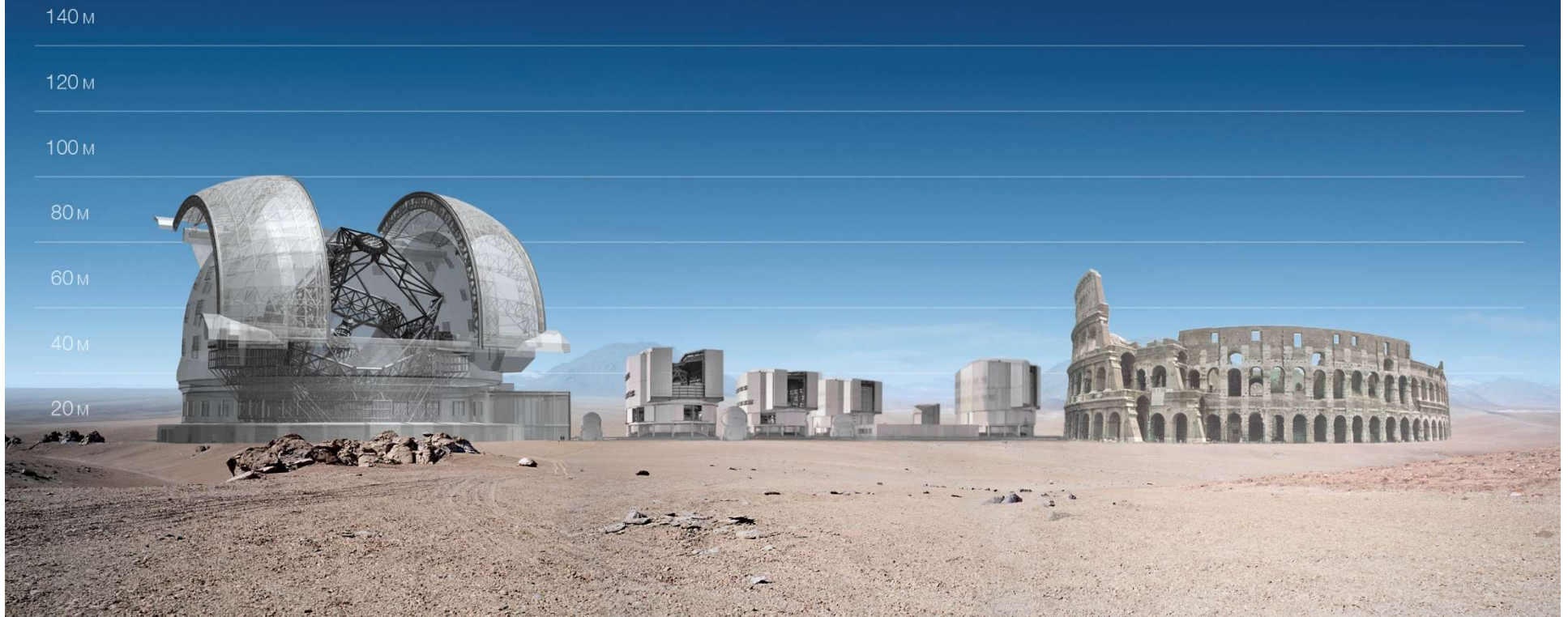
## Interactions btw notches and defects



# Additive Materials

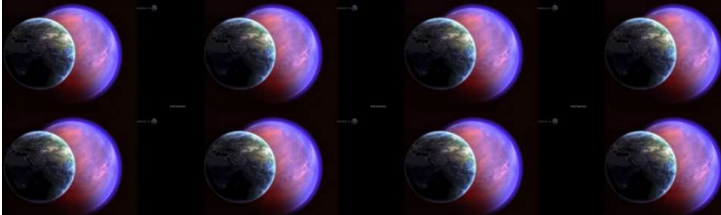
## Interactions btw notches and defects





**EUROPEAN-EXTREMELY LARGE TELESCOPE (E-ELT) 1.200.000 weldments, 1.500.000 notches**

**8 new Twin Earths**

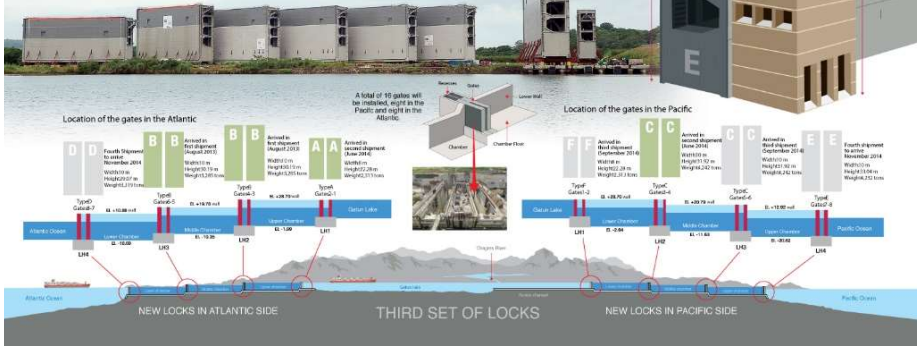


# STEELGIANTS

The new locks of the Panama Canal will have 16 rolling gates, fabricated in Italy by Cimolai SpA. The gates have been arriving to Panama since August 2013 in staggered shipments of four at a time. The rolling system facilitates gate maintenance.

All gates are the same weight: 37,000 tons

The tallest of all gates is 33.04 meters high, the equivalent of an 11-story building



Department of Mechanical Engineering



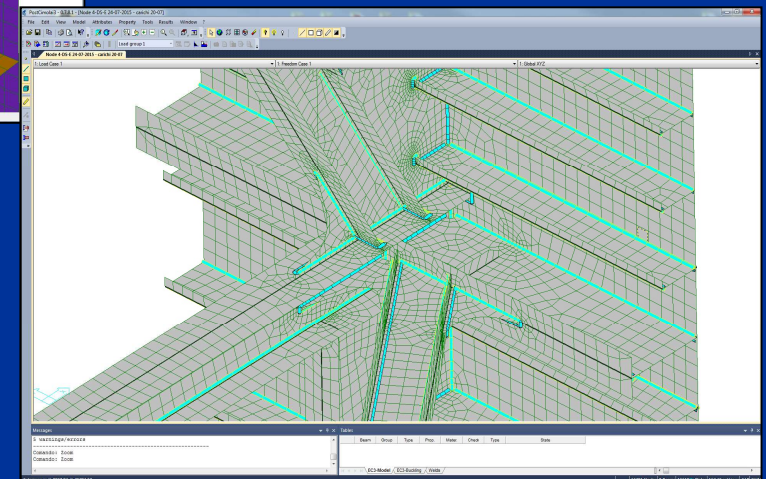
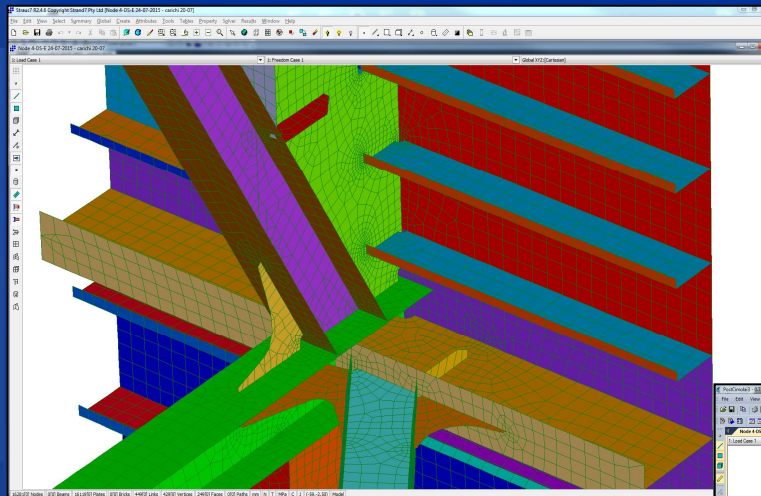
Very proud!!!! (design of the gates and of the ships for the transportation 10.000 Km by sea)  
Cimolai has financed 5 PhD (500 KEuro) and employed 10 master students opening a research centre dedicated to advanced structural problems

# AUTOMATIC FATIGUE CHECK OF WELDS AND NOTCHES



Department of Mechanical Engineering

Dedicated post-processor for massive fatigue check of weldings, notches and base material.

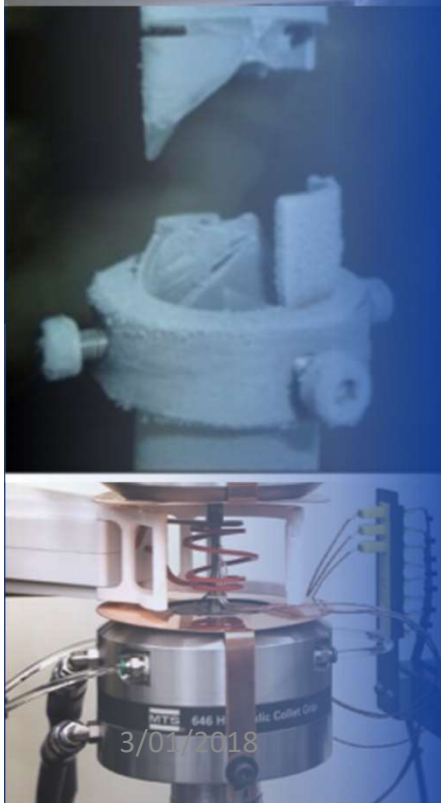


## ❑ AUTOMATED APPROACHES:

- Nominal stress
- Modified nominal stress
- SED and N-SIF (shell element based)
- Hot-Spot stress

## ❑ IMPLEMENTED STANDARDS:

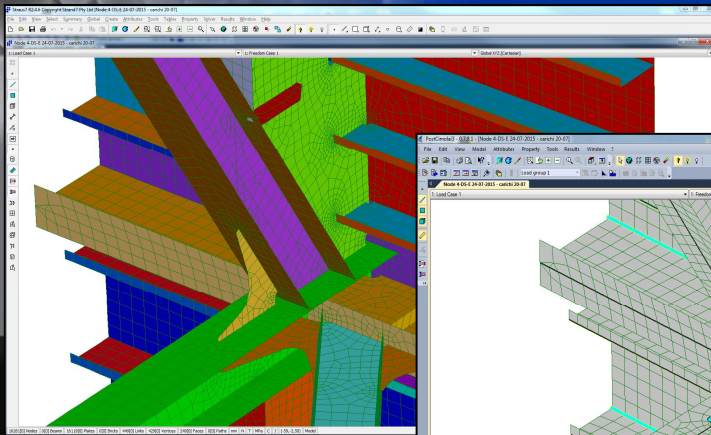
- Eurocode 3 - Design of steel structures: Fatigue
- IIW - Recommendations for fatigue design of welded joints, Hobbacher
- EN 13445 - DNV-GL (Hot Spot user defined)



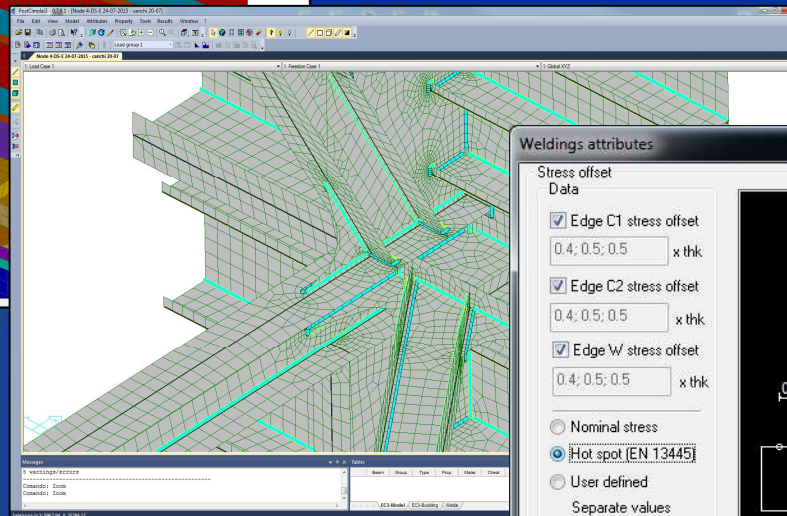


# AUTOMATIC FATIGUE CHECK OF WELDS AND NOTCHES

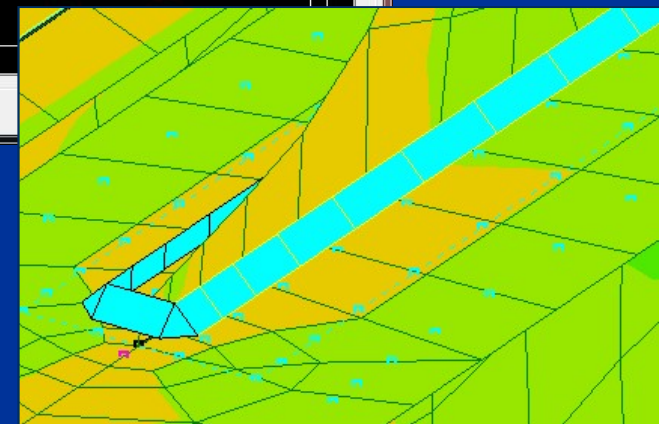
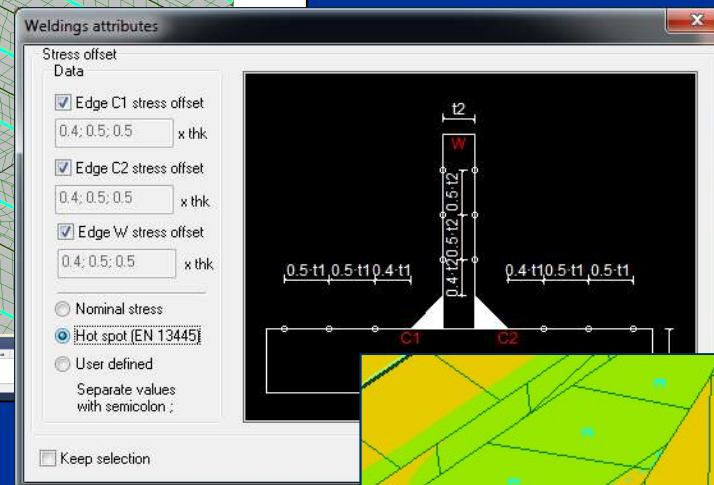
## 1. Definition of a shell finite element model



## 2. Automatic finding of check lines in the postprocessor

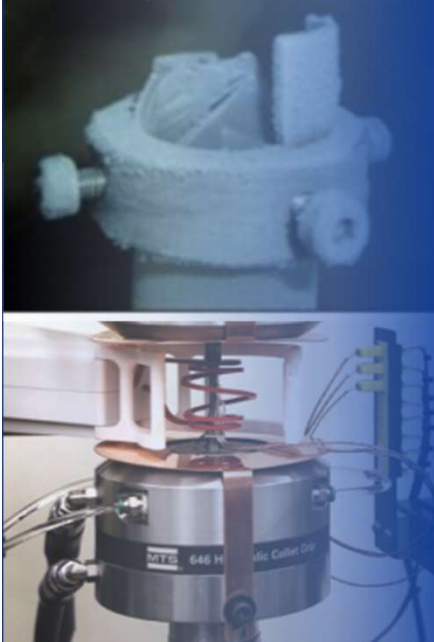


## 3. Set of offsets to stress reading

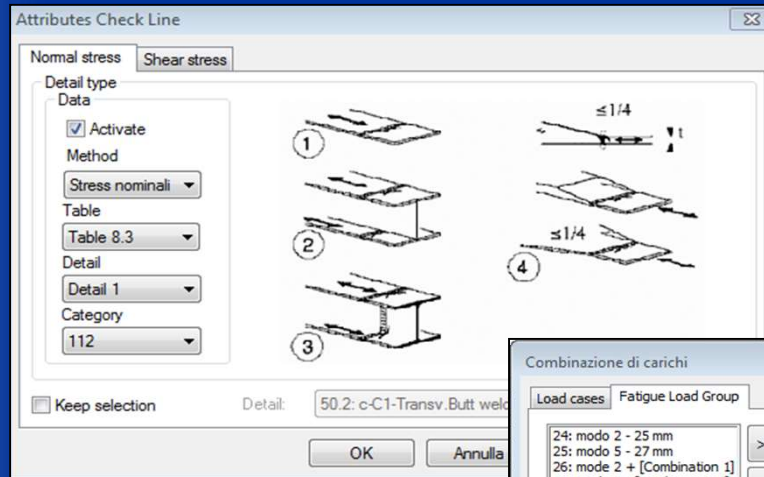


### OFFSET STRESS READING:

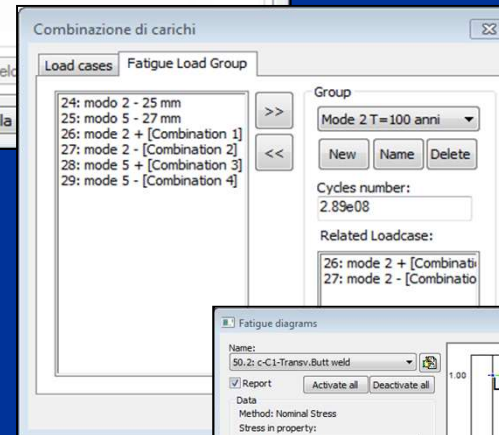
- ✓ Nominal stress: default 1.5t (DVS 1612 and Hobbacher)
- ✓ Hot-Spot stress: default 0.4t;0.5t;0.5t (EN 13445)
- ✓ User defined (SED and other local approaches)



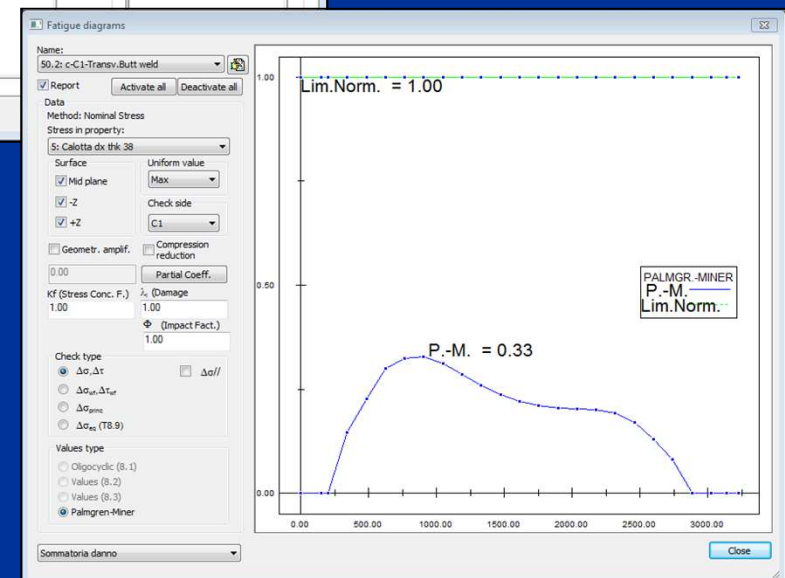
## 4. Set the fatigue class details



## 5. Load spectrum



## 6. Fatigue check



# Additive Materials



Department of Mechanical Engineering

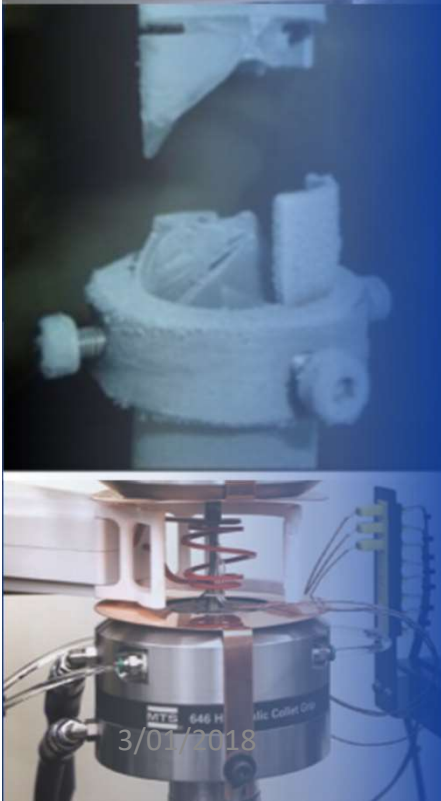


ESIS Technical committee 15 (Chief)  
ESFRI HORIZON 2020 PROPOSAL (180 ME, 13  
PARTNERS)



## The fatigue behaviour of Ti6Al4V under multi-axial loading and in presence of notches was investigated

- The nominal load ratio was found to have a great influence on the fatigue strength while the influence of the load phase angle seems to be limited
- The re-analysis of the fatigue data in terms of the strain energy density range at the notch tip allowed us to summarise all the multiaxial data on notched specimens in a single fatigue scatter band
- The proposed approach results therefore a very useful tool for the fatigue analysis of components subjected to multiaxial fatigue loading in the presence of severe notches





**You are also welcome  
in Norway!!!**



# INTERNATIONAL SYMPOSIUM FOR PRODUCTION RESEARCH 2017

## “Transition to Industry 4.0”

13-15 September 2017, Vienna



TECHNISCHE  
UNIVERSITÄT  
WIEN

### ISPR 2017

13-15 September 2017, Vienna



Üretim Araştırmaları  
Derneği



3/01/2018

62



**MANY THANKS  
FOR THE KIND INVITATION**

**HONORED AND GRATEFUL TO BE HERE**

*it was better to meet you at least once  
then never have met you*

**‘My favorite things in life don't cost any  
money. It's really clear that the most  
precious resource we all have is time’**